# Hybrid machine-learning and first-principles design for transition metal complexes

Jon Paul Janet <sup>1</sup> Chenru Duan<sup>2</sup> Aditya Nandy<sup>2</sup> Heather Kulik <sup>1</sup>

<sup>1</sup>Department of Chemical Engineering, Massachusetts Institute of Technology

<sup>2</sup>Department of Chemistry, Massachusetts Institute of Technology

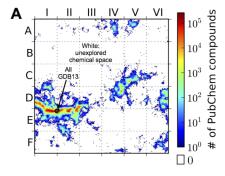


Foundational & Applied Data Science for Molecular and Material Science & Engineering

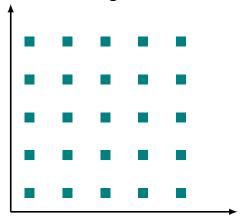
#### How can we design new materials using computers?

The space of possible chemistries is incredibly vast, with  $\mathcal{O}(10^{60})$  small organic molecules.

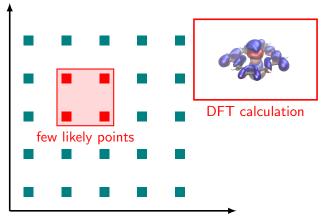
All potentially undiscovered medicines, catalysts and materials are somewhere, out in this huge space.



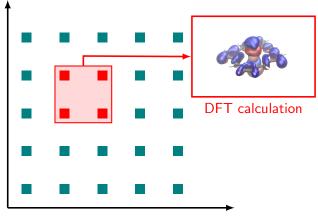
Virshup et al., J. Am. Chem. Soc., 135(19): 7296-7303, 2013.



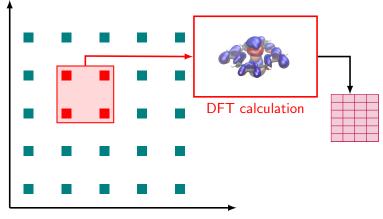
Chemical Design Space  $C_f$ 



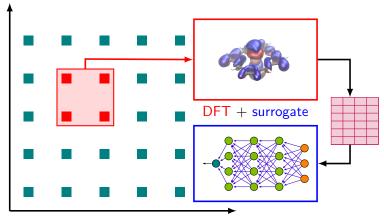
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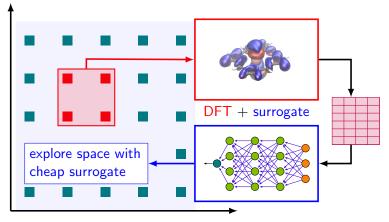
Chemical Design Space  $C_f$ 



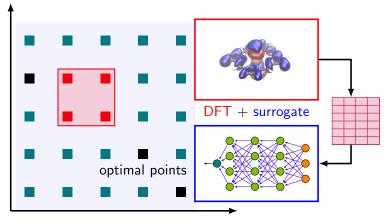
Chemical Design Space  $C_f$ 



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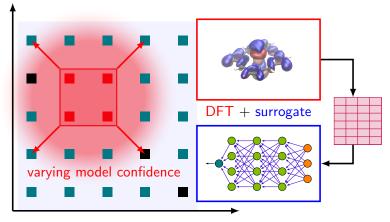


Chemical Design Space  $C_f$ 



Chemical Design Space  $C_f$ 

Introduction

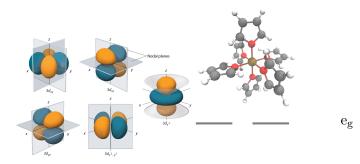


Chemical Design Space  $C_f$ 

Introduction 0000

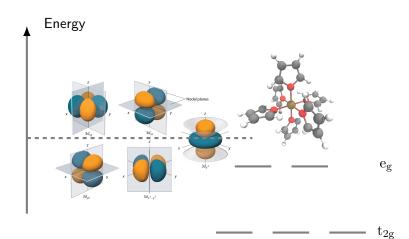


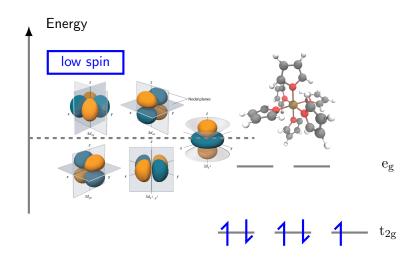
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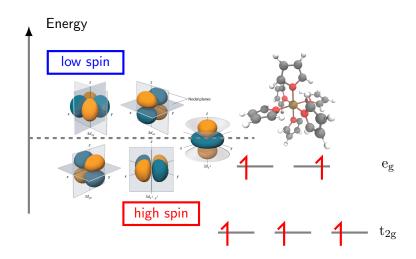


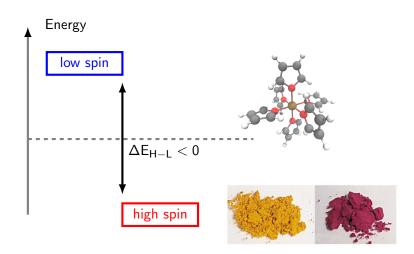
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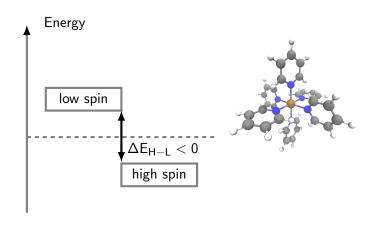
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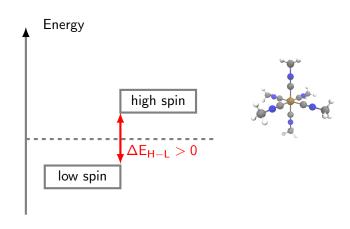




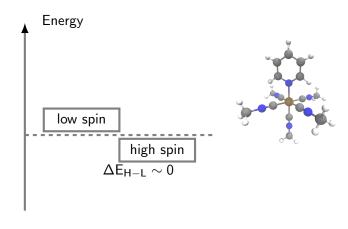




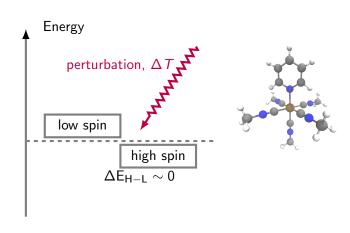
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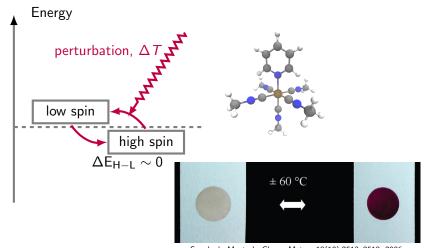
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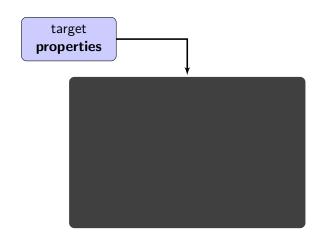
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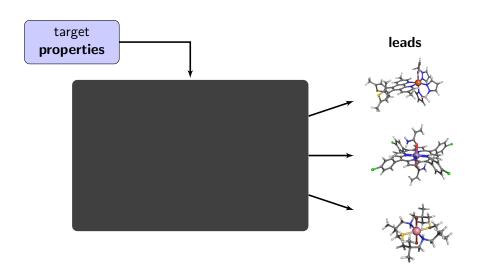


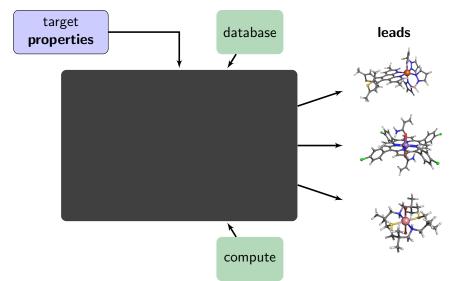
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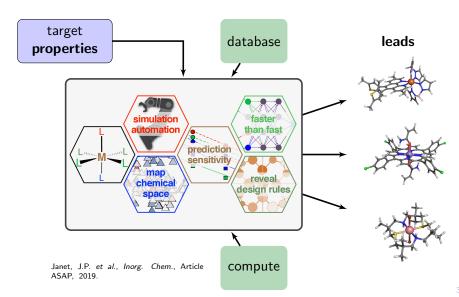


target properties

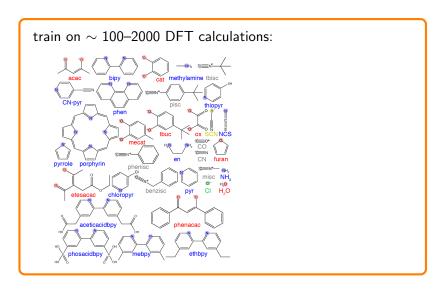


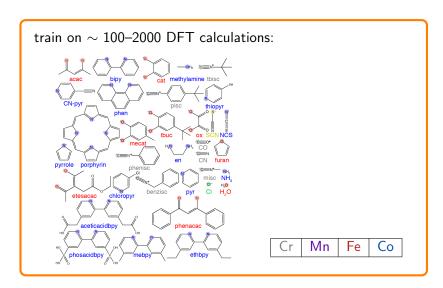


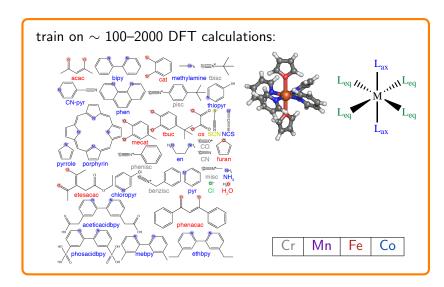


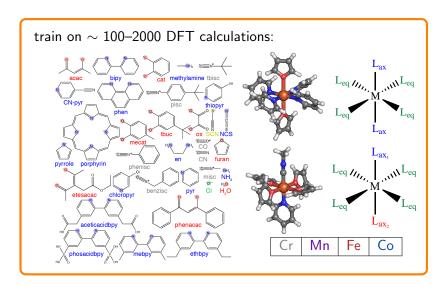


train on  $\sim$  100–2000 DFT calculations:



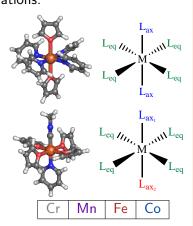


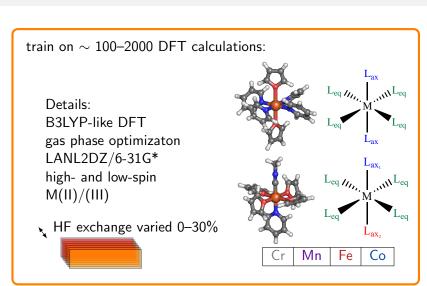




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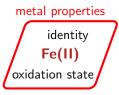
Details: B3LYP-like DFT gas phase optimizaton LANL2DZ/6-31G\* high- and low-spin M(II)/(III)

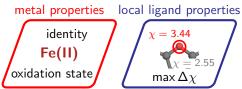




# Modeling of TM complexes with heuristic representations

First attempt using simple features inspired by inorganic chem:







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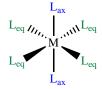


mixed continous discrete ligand-centered: MCDL-25

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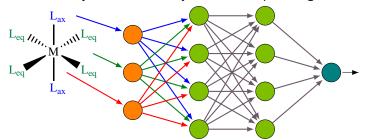
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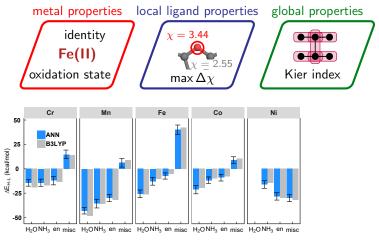


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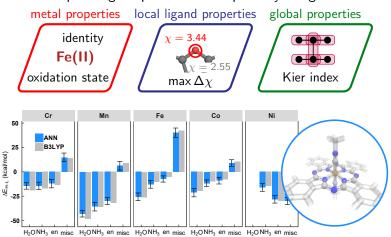
fully-connected 2-layer ANN, dropout regularization



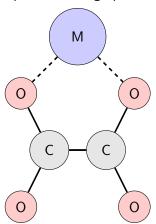


Janet, J.P. and Kulik, H.J., Chem. Sci., 8:5137-5152, 2017.

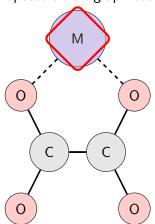
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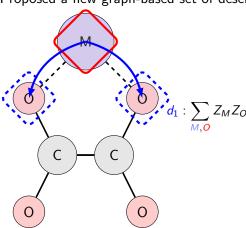
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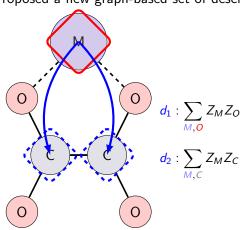
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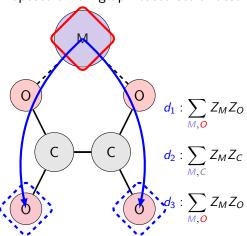
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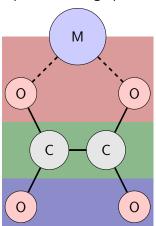
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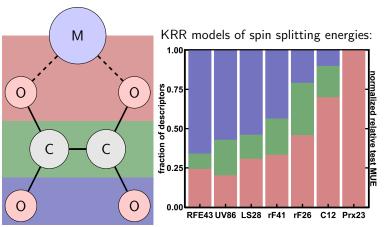
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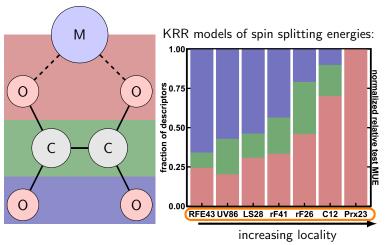
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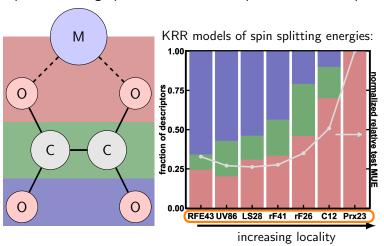
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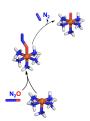
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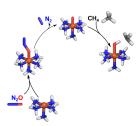
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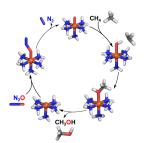


Can we apply the same ideas to cheaply predict catalytically-relevant properties?

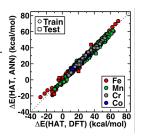


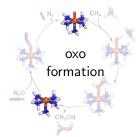
Nandy, A. et al., in preparation.

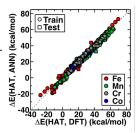
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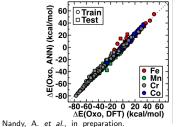


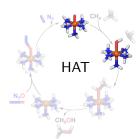
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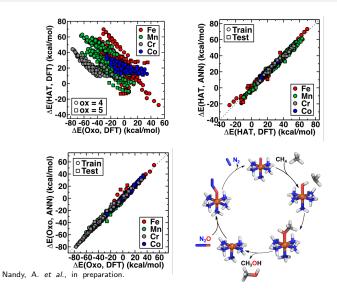










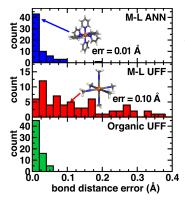


#### Machine learning job initialization

Metal-ligand bonding is difficult to resolve without QM:

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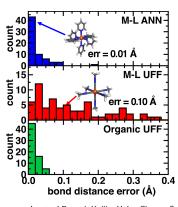


we can predict bond lengths

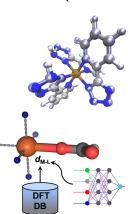
Janet, J.P. and Kulik, H.J., Chem. Sci., 8:5137–5152, 2017.
Janet, J.P. et al., Ind. Eng. Chem. Res., 56(17):4898–4910, 2017.
Janet, J.P. et al., Inorg. Chem., Article ASAP, 2019.

## Machine learning job initialization

Metal-ligand bonding is difficult to resolve without QM:



we can predict bond lengths and use this to intialize new calculations



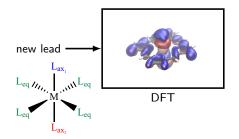
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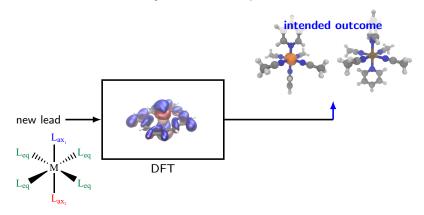
However, even with this, DFT job failure is a frequent issue:

#### new lead

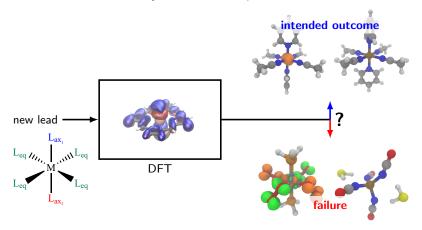


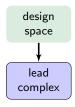
# Beyond prediction: live job management

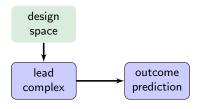




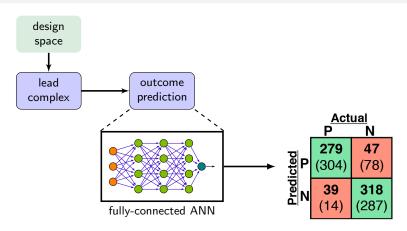
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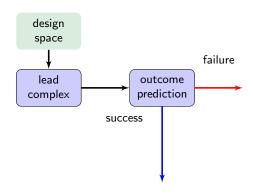


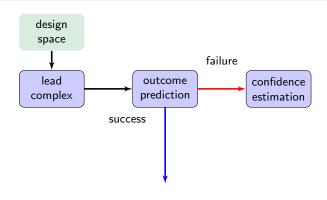


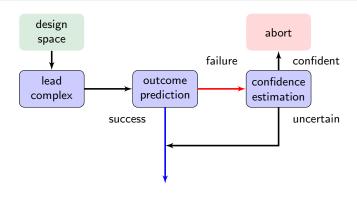


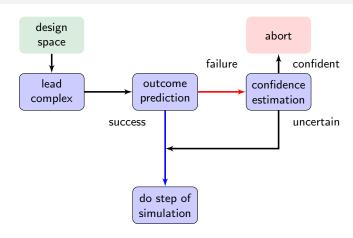
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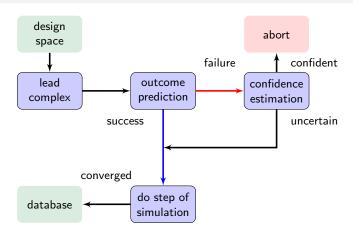


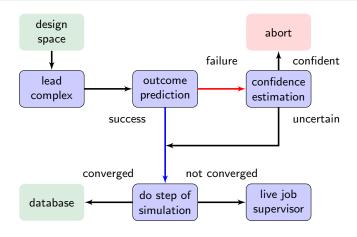


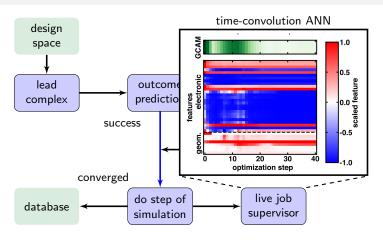


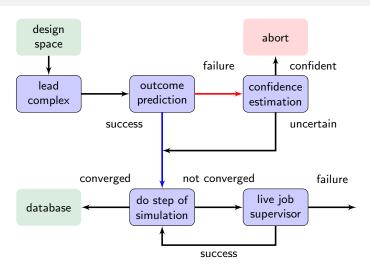




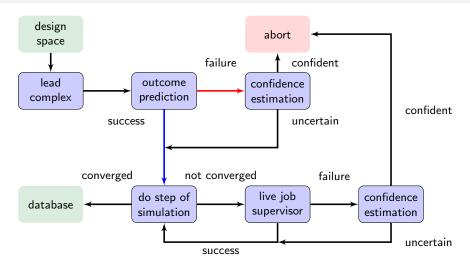




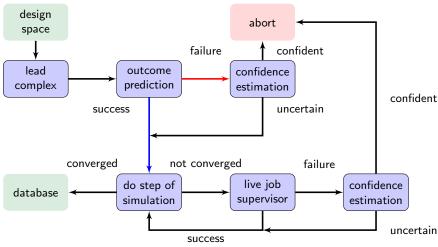




Duan, C., Janet, J.P. et al., J. Chem. Theory. Comp., 15(4):2331-2345, 2019.



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This leads to about 40% time savings and can abort almost all failures.

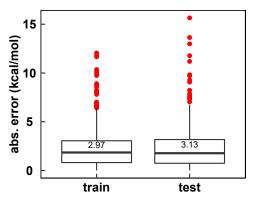
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Test-set performance is not necessarily a good metric for general transferability<sup>1</sup>:

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### Model transferability

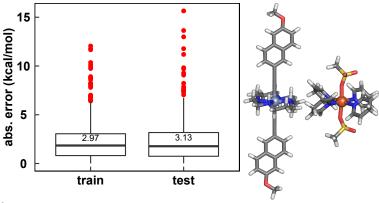
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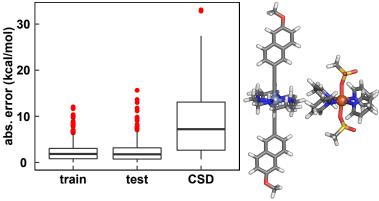
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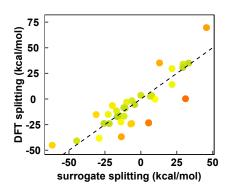
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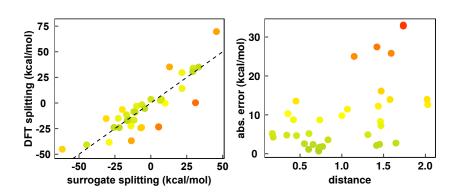


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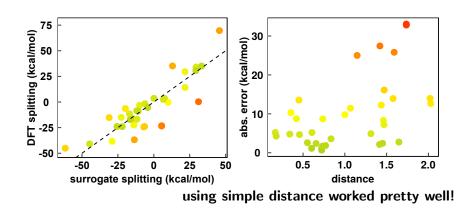
# System-specific generalization



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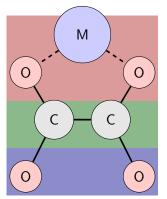
#### System-specific generalization



Results are worse for more complex representations<sup>1</sup>:

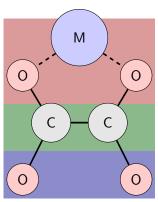
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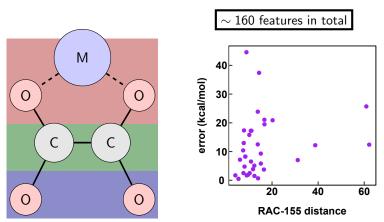
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 $\sim$  160 features in total

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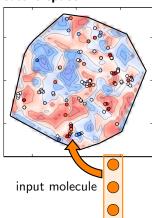
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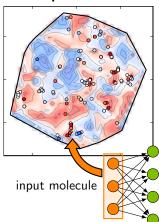
<sup>&</sup>lt;sup>1</sup> Janet, J.P., and Kulik, H.J., J. Phys. Chem. A 121(46):8939-8954, 2017.



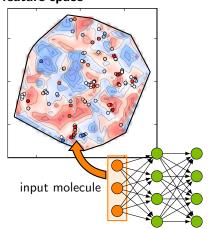
#### feature space

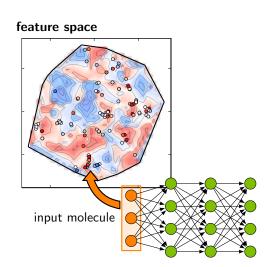


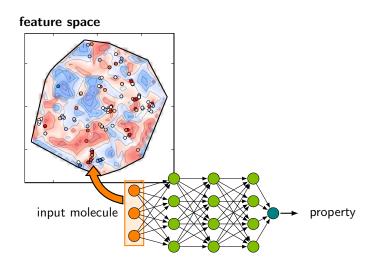
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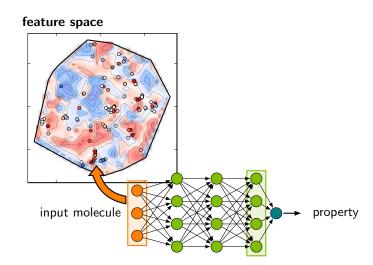


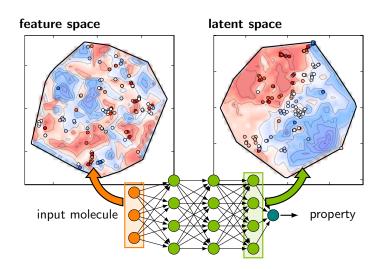
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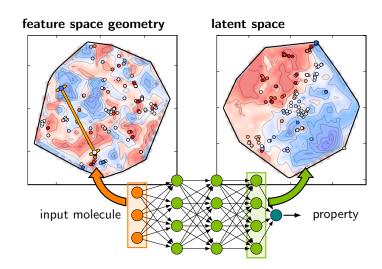


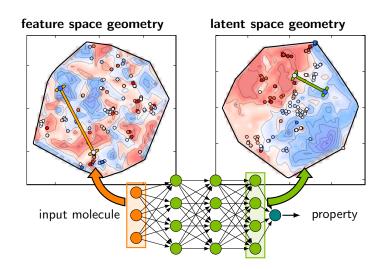












# Other UQ metrics

1) Data-sampling ensembles:

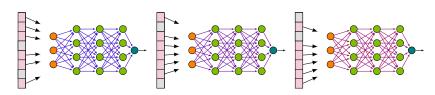
# Other UQ metrics

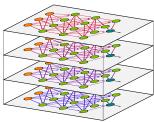
1) Data-sampling ensembles:



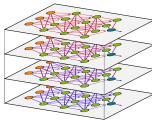
# Other UQ metrics

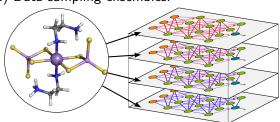
1) Data-sampling ensembles:

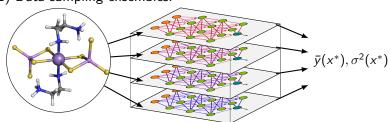




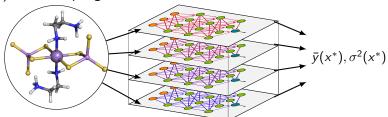








1) Data-sampling ensembles:



2) Monte Carlo dropout<sup>1</sup>:



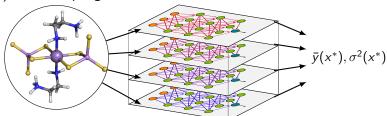




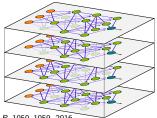
<sup>&</sup>lt;sup>1</sup>:Gal, Y. and Ghahramani, Z., ICMLR, 1050-1059, 2016.

#### •

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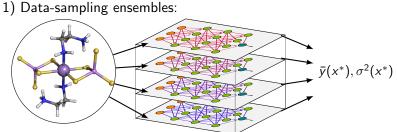


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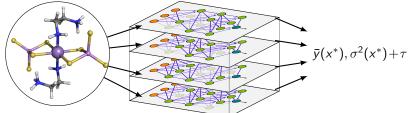


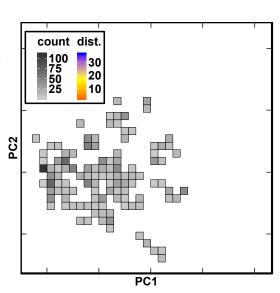
<sup>&</sup>lt;sup>1</sup>:Gal, Y. and Ghahramani, Z., ICMLR, 1050-1059, 2016.

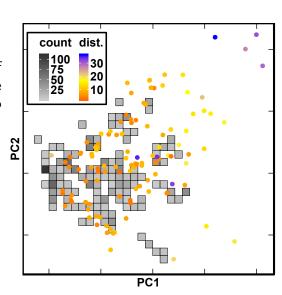
#### 1) 5

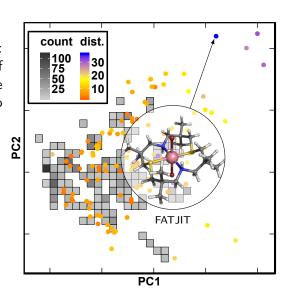


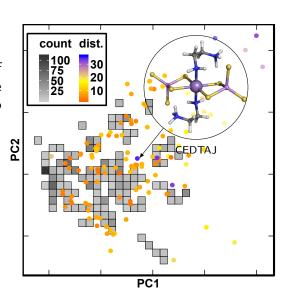
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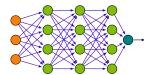


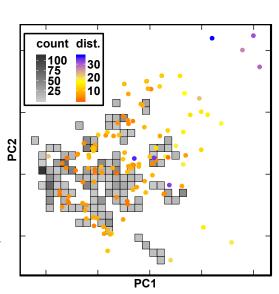




'Out-of-distribution' test: spin-splitting energies of 116 structures from the CSD, from training-like to very different.

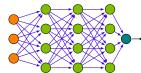
Train 3-layer fully connected ANN on 1900 DFT results on simple ligands:

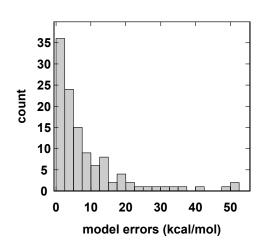




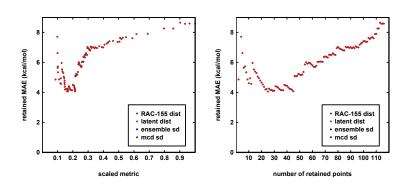
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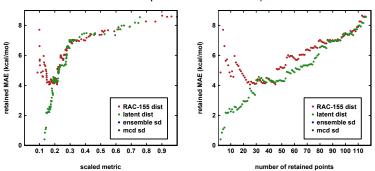
Make a comparison of discriminative power<sup>1</sup>:



Janet, J.P., et al., ChemRxiv, 10.26434/chemrxiv.7900277.v1.

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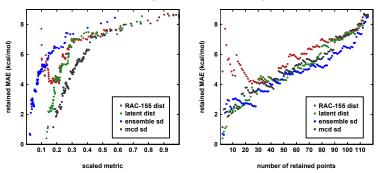
latent distances are superior to feature space distances



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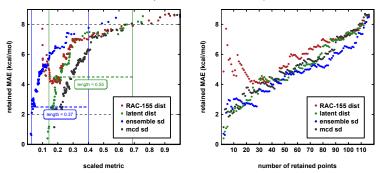


comparable with ensembles and mc dropout

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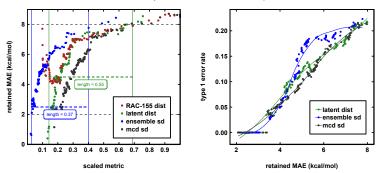


comparable with ensembles and mc dropout stability is important

<sup>&</sup>lt;sup>1</sup> Janet, J.P., et al., ChemRxiv, 10.26434/chemrxiv.7900277.v1.

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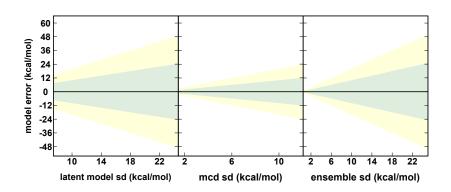
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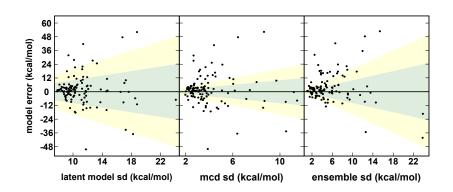
$$\varepsilon(d) \sim \mathcal{N}\left(0, \sigma_1^2 + d\sigma_2^2\right)$$



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## How do these distributions compare?

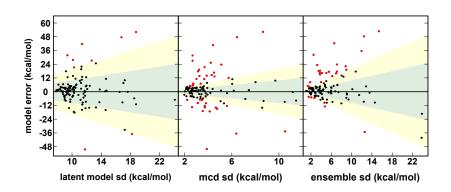
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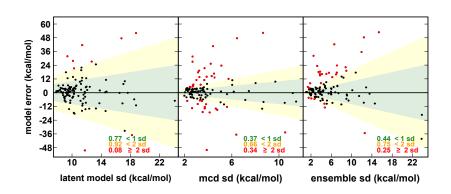
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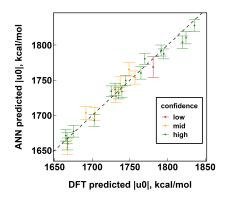
#### QM9 results

Similar error control can be obtained for QM9 benchmark organic data<sup>1</sup>. We train on 5% and make predictions on 95%.

<sup>&</sup>lt;sup>1</sup> Ramakrishnan, R., et al., Sci. Data, 1, 2014.

#### QM9 results

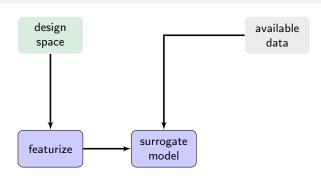
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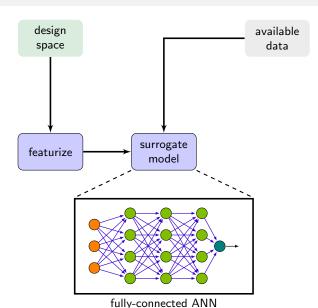


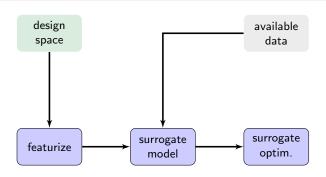
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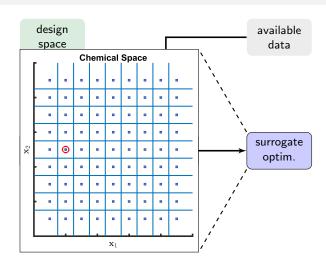
design space

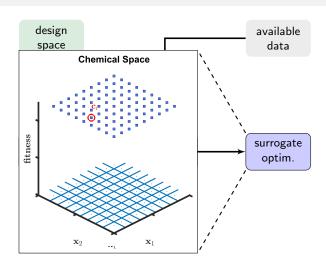


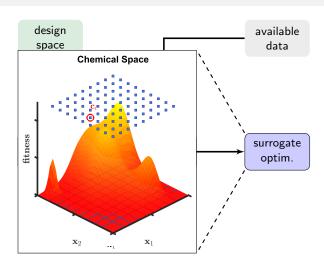


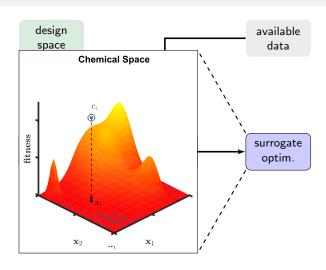


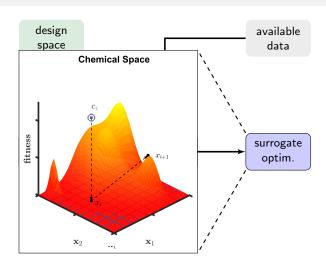


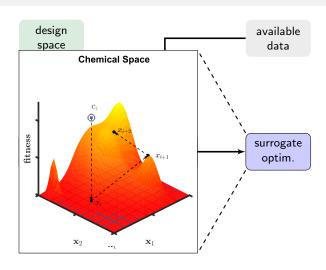


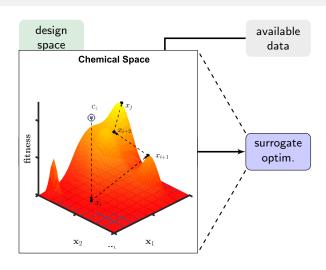




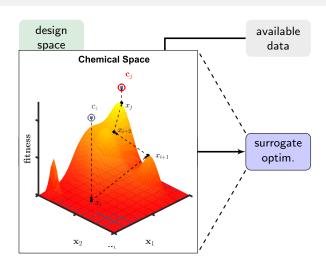




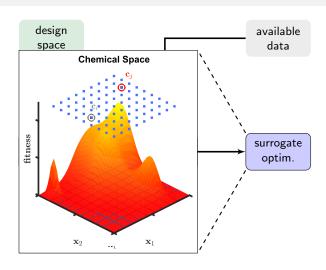




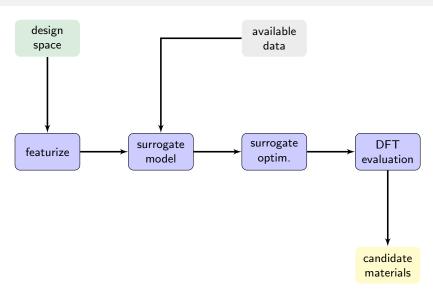
candidate materials

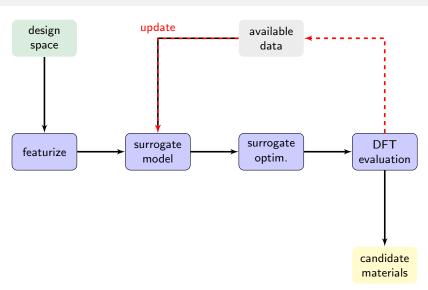


candidate materials



candidate materials





Can we use the ANN model to find new spin-crossover materials, i.e.  $\Delta E_{H-L} = 0$ ?

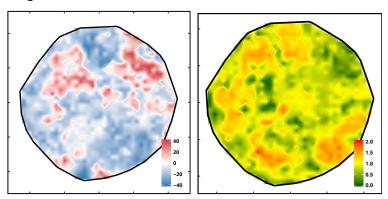
<sup>&</sup>lt;sup>3</sup>Janet, J.P., Chan, L. and Kulik, H.J., *J. Phys. Chem. Lett.*, 9(5):1064–1071, 2018.

Can we use the ANN model to find new spin-crossover materials, i.e.  $\Delta E_{H-L}=0?$  Define an expanded space with <2% training coverage  $^3$ 

<sup>&</sup>lt;sup>3</sup>Janet, J.P., Chan, L. and Kulik, H.J., *J. Phys. Chem. Lett.*, 9(5):1064–1071, 2018.

#### Can we use these models for discovery?

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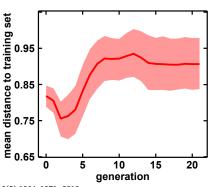


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### UQ and evolutionary design

We developed an evolutionary algorithm that combines uncertainty estimation with property prediction:

At high distances, surrogate is unreliable. At low distance, data is weakly informative.



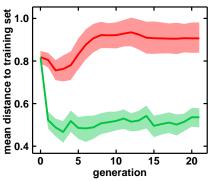
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$$\begin{array}{l} F_{s+d}(x) & := \\ \exp\left[-\left(\frac{\Delta E_{\text{H-L}}(x)}{P\Delta E_{\text{H-L}}}\right)^2\right] \exp\left[-\left(\frac{d(x)}{Pd}\right)^2\right] \end{array}$$



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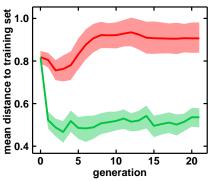
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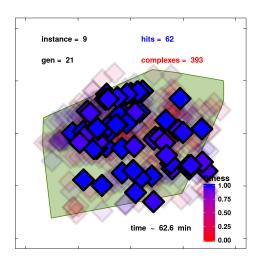


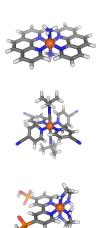
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#### Demonstration

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#### **Demonstration**

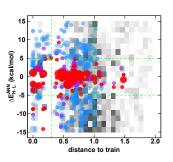




#### Discovery results

#### Spin splitting design:

- We combine ANN predictions and uncertainties using an evolutionary algorithm.
- Error control allows 60% of leads to be validated with DFT.<sup>1</sup>



<sup>&</sup>lt;sup>1</sup> Janet, J.P., Chan, L. and Kulik, H.J., *J. Phys. Chem. Lett.*, 9(5):1064–1071, 2018.

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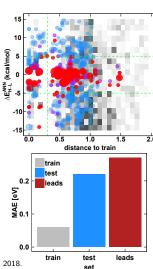
Error control allows 60% of leads to be validated with DFT.<sup>1</sup>

#### Frontier orbital properties:

This approach also works for frontier orbtial design<sup>2</sup>, obtaining average HOMO of 3.98 eV compared to target 4.00 eV.

<sup>&</sup>lt;sup>1</sup> Janet, J.P., Chan, L. and Kulik, H.J., *J. Phys. Chem. Lett.*, 9(5):1064–1071, 2018.

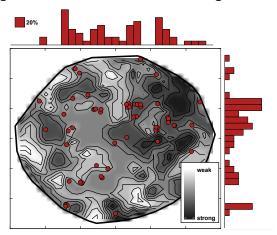




Because we have trained our models on varying with exact exchange, we can tune functionals for design:

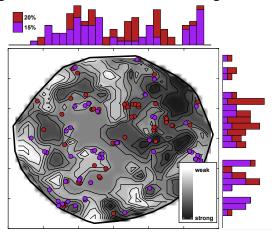
# Hedging against DFT uncertainty

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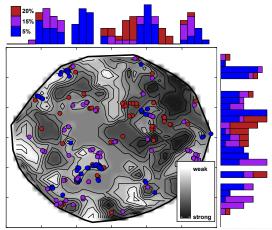
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## Hedging against DFT uncertainty

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Awkward roommates or match made in heaven?

#### physics-driven



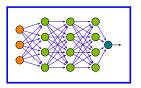
slow, accurate (?)

Awkward roommates or match made in heaven?

#### physics-driven

#### data-driven





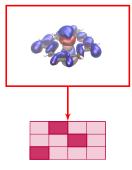
slow, accurate (?)

fast, uncertainty-aware

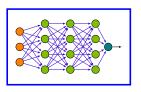
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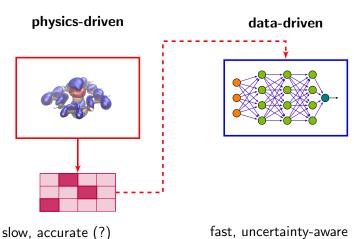
## data-driven

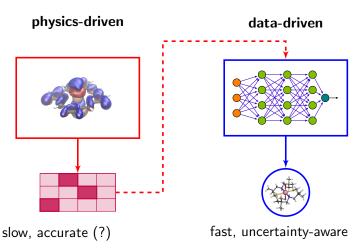


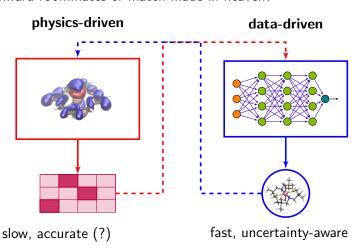
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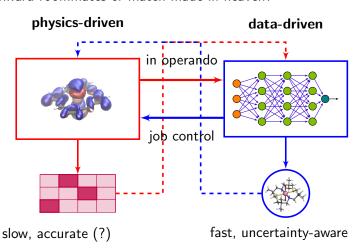


fast, uncertainty-aware









#### Thanks to the Kulik group and funding partners:

