

# Multi-Objective, Machine-Learning Assisted First-Principles Design of Transition Metal Complexes for Redox Couples

Jon Paul Janet<sup>1</sup> Heather Kulik<sup>1</sup>

<sup>1</sup>Department of Chemical Engineering, Massachusetts Institute of Technology



Applications of Data Science in Molecular Sciences I

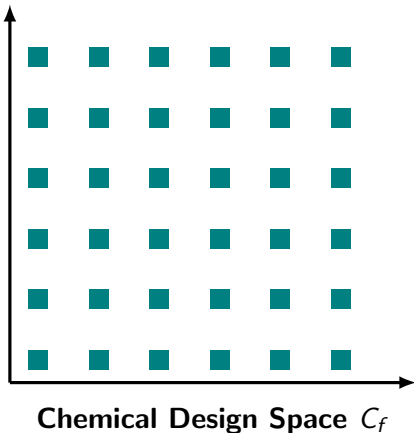
11.11.19

# Motivation: chemical discovery

**How can we design new materials using computers?**

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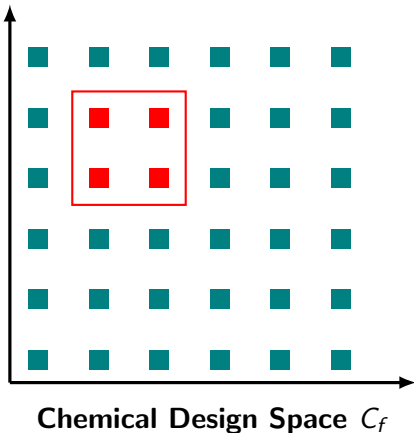
How can we design new materials using computers?



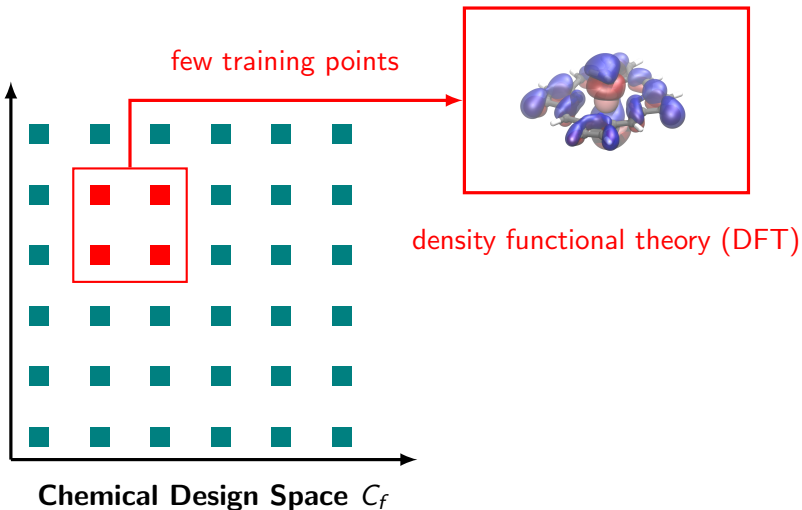
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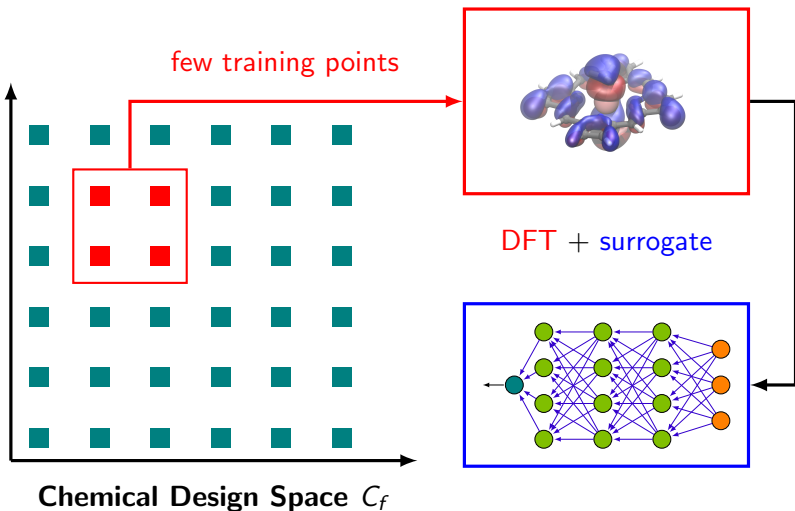
few training points



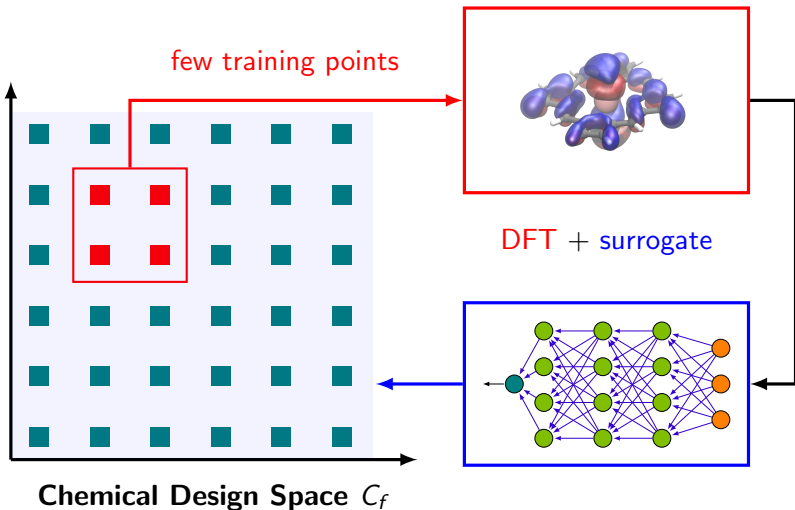
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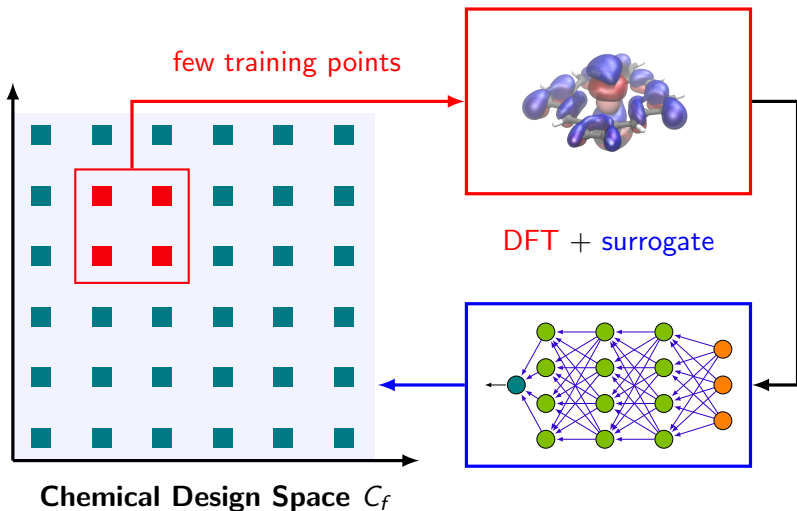
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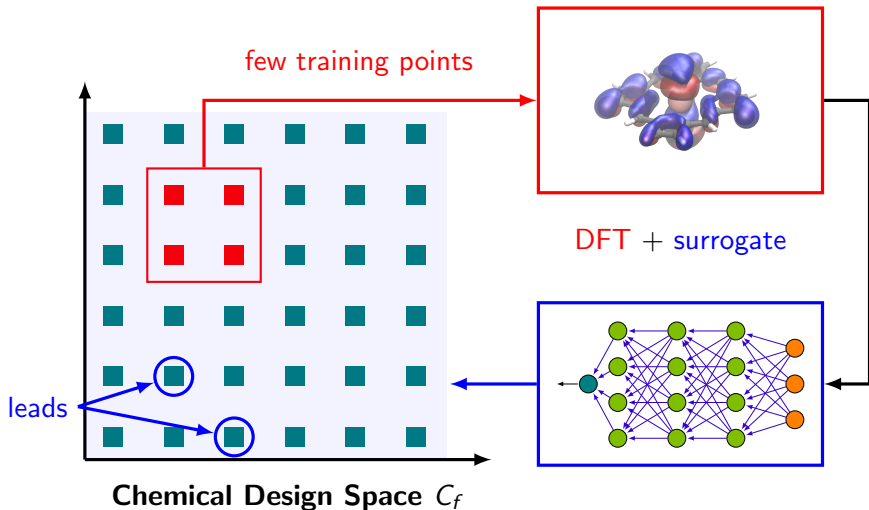


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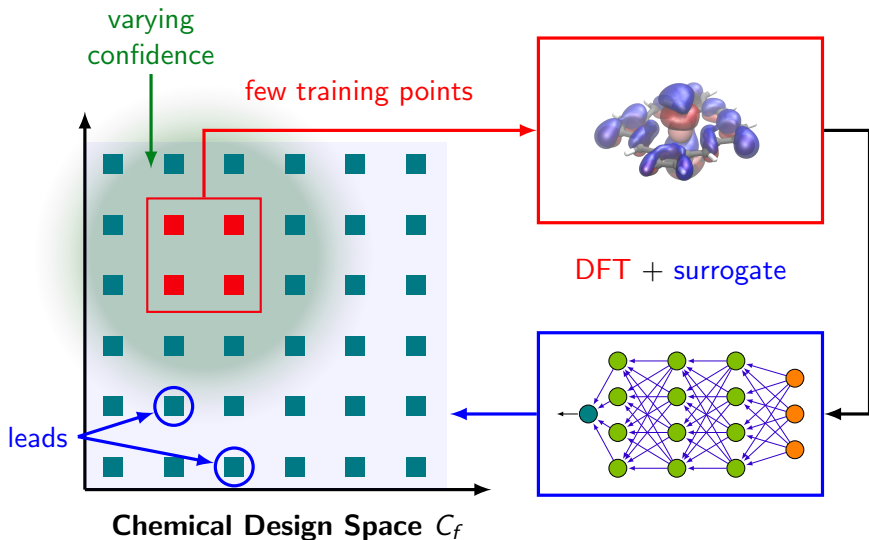




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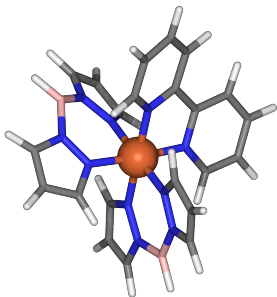


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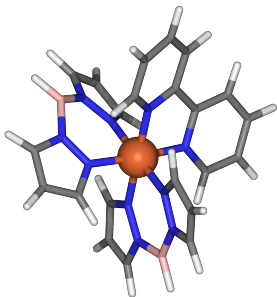
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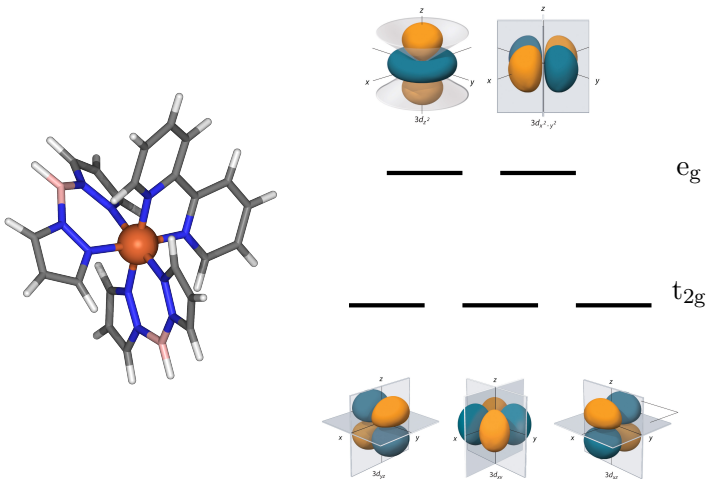
# Transition metal complexes

Difficult chemistry with multiple spin & oxidation states!



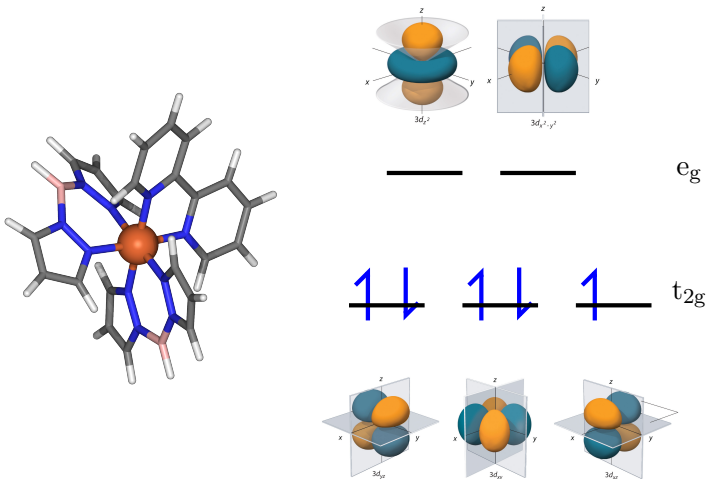
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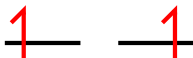
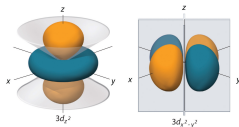
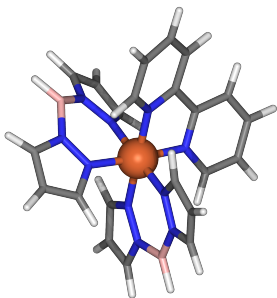
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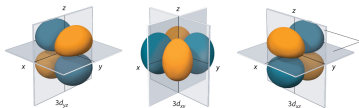
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$e_g$



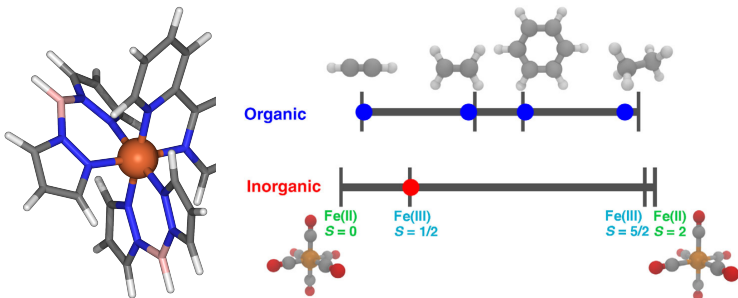
$t_{2g}$





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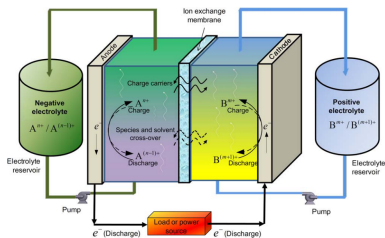


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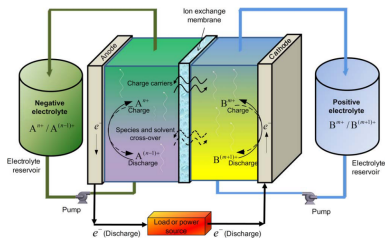


Perry, M.L. and Adam, Z., *J. Electrochem. Soc.*, 163(1):A5064–A5067, 2018.

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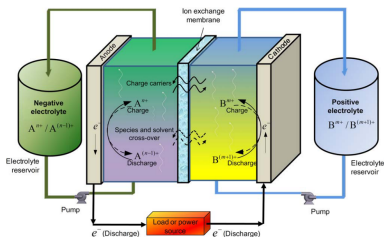
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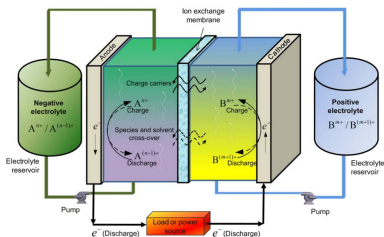
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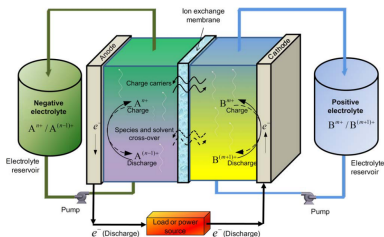
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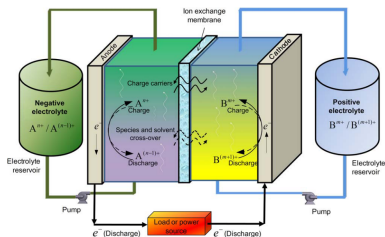
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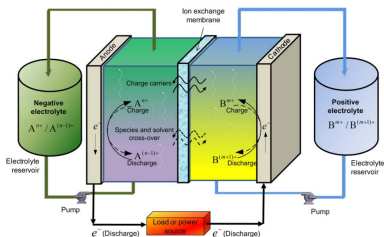
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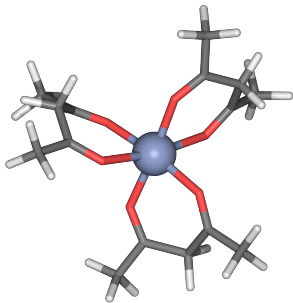
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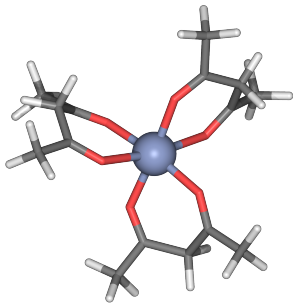
We need complexes that have high redox potential **and** good solubility

# First principles methods

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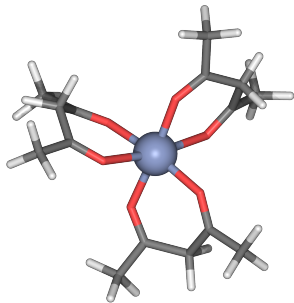
# First principles methods



Metals:

Cr	Mn	Fe	Co
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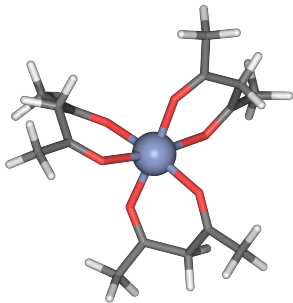


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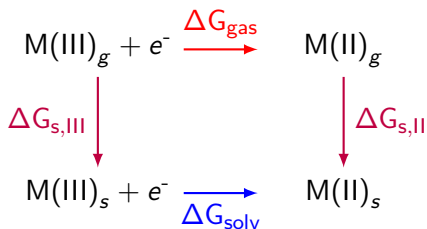


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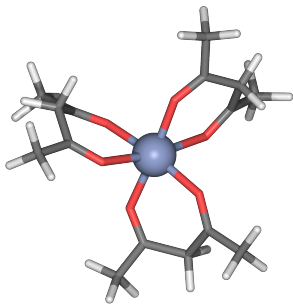


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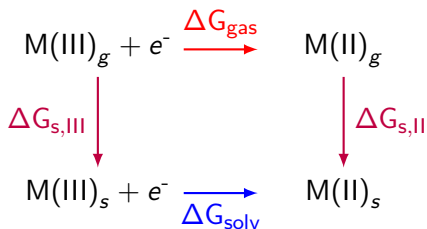


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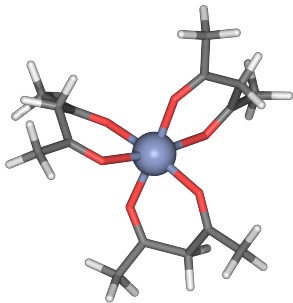
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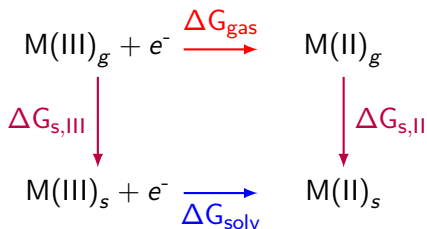
$$\log P \approx \log \frac{\Delta G_{s,\text{II,octanol}}}{\Delta G_{s,\text{II,water}}}$$

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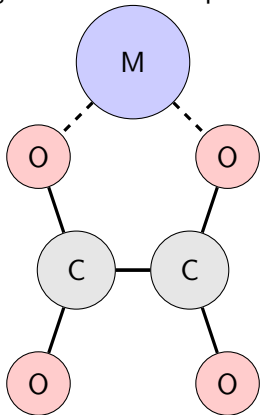
- B3LYP-like DFT
- gas phase optimizations
- LANL2DZ/6-31G\*
- COSMO solvent,  $\epsilon = 78.39$  or  $10.30$
- high- and low-spin



# Machine learning methods

## Featurization:

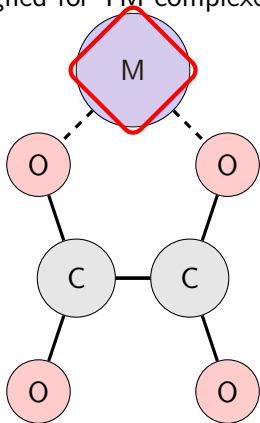
Graph-based features (RACs)  
designed for TM complexes:



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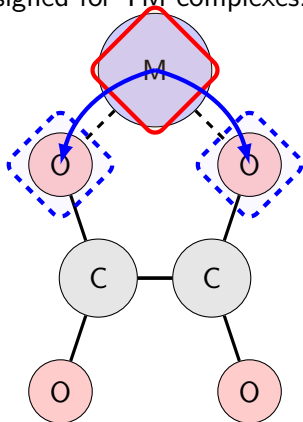
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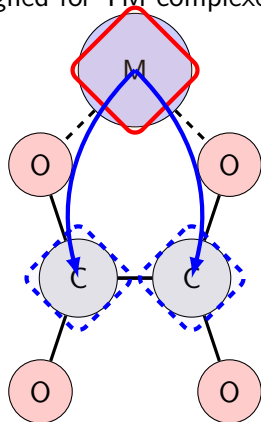


$$d_1 : \sum_{M,O} Z_M Z_O$$

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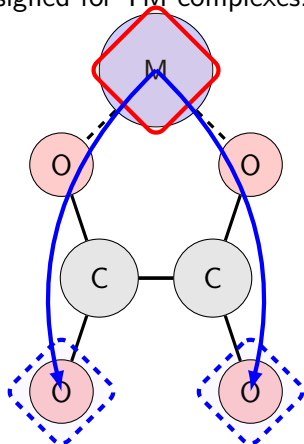
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$$d_2 : \sum_{M,C} Z_M Z_C$$

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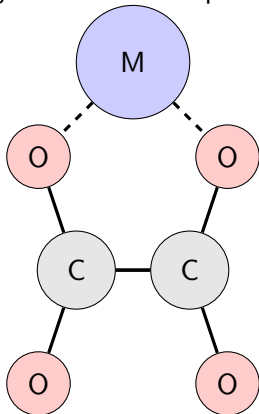
$$d_2 : \sum_{M,C} Z_M Z_C$$

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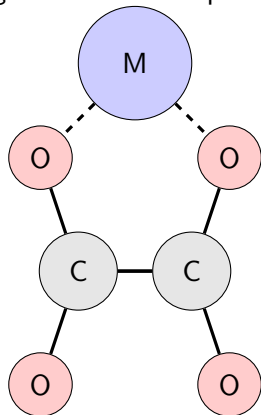
Janet, J.P., and Kulik, H.J., *J. Phys. Chem. A*, 121(46):8939–8954, 2017.

## Regression:

# Machine learning methods

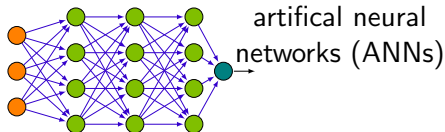
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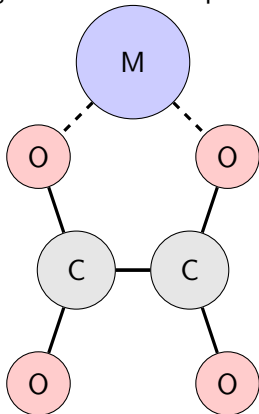
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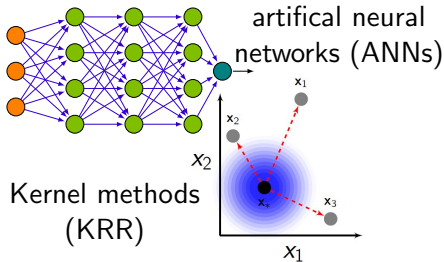
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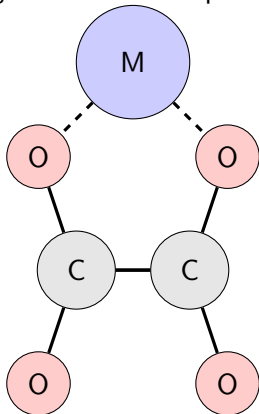




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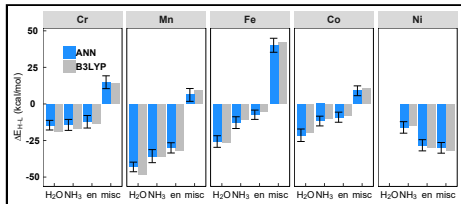
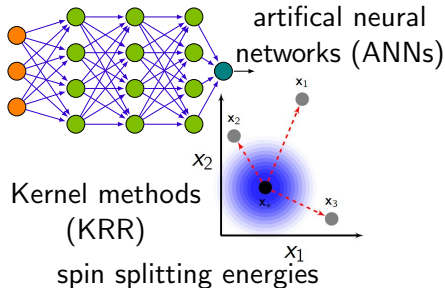
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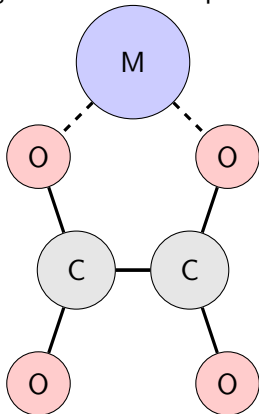


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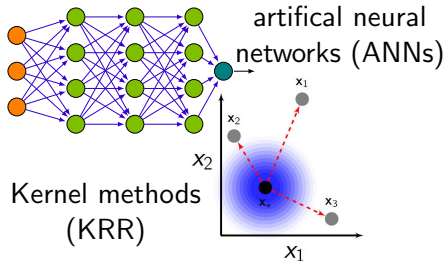
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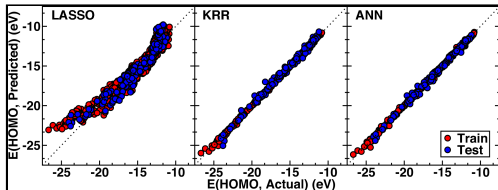
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## Regression:



Kernel methods (KRR)

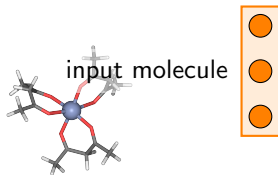
frontier orbital properties



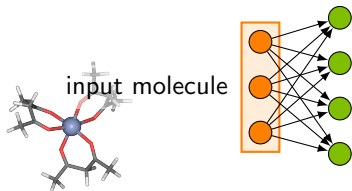
Nandy, A. et al., *Ind. Eng. Chem. Res.*, 57(42):13973–13986, 2018.

# Latent distance similarity

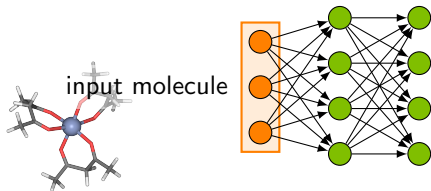
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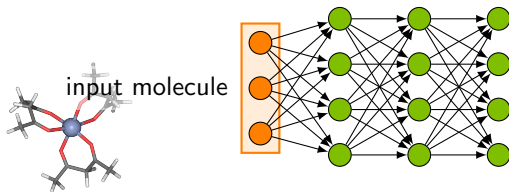
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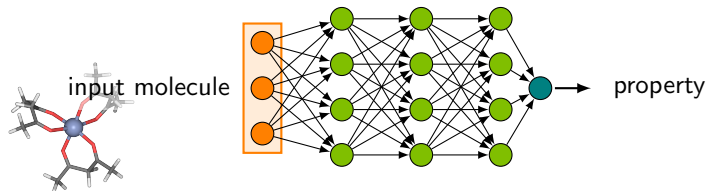
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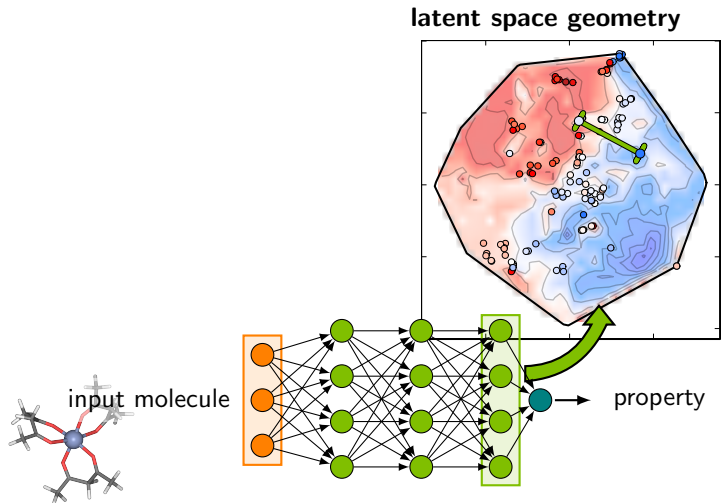


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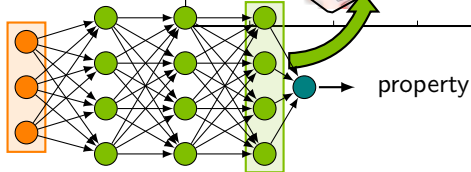
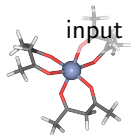


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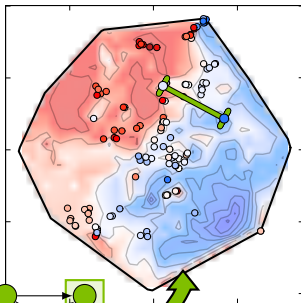
Proposed a simple probabilistic error model based on latent distance to training data,  $d$ :

$$\varepsilon(d) \sim \mathcal{N}(0, \sigma_1^2 + d\sigma_2^2)$$

Estimate  $\sigma_1$ ,  $\sigma_2$  by log likelihood



latent space geometry

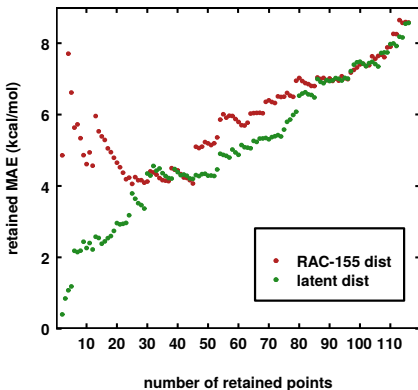


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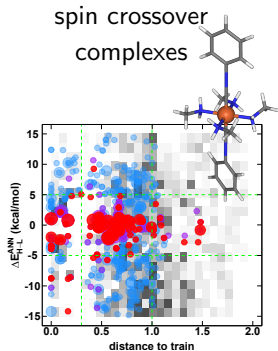


## Using models for discovery

We have used evolutionary algorithms for uncertainty-aware design for TM complexes:

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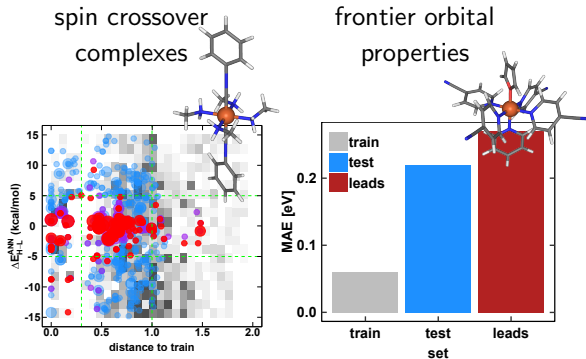
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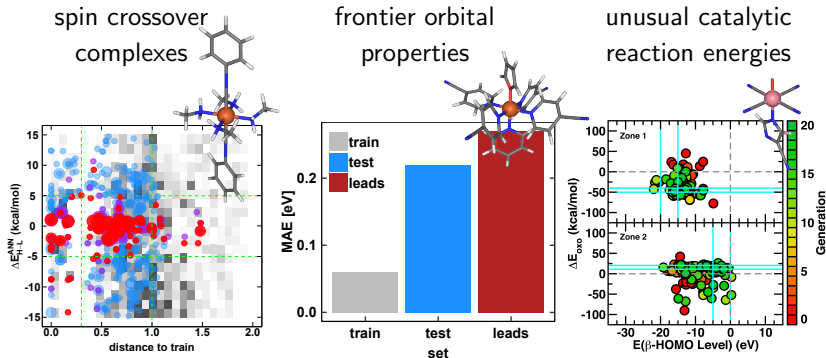
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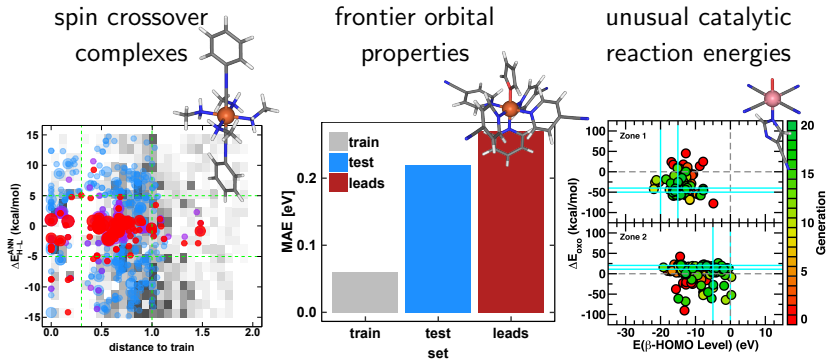
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443e: Aditya Nandy: Wednesday, 9:12 (Peacock Spring)

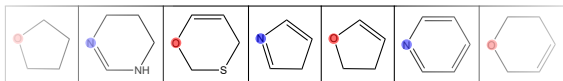


# A design space for RFBs

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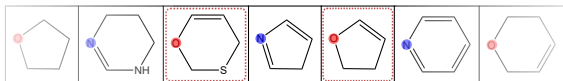


# A design space for RFBs



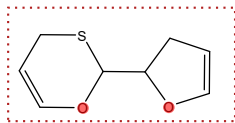
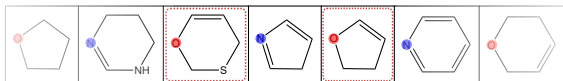
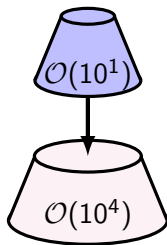
40 heterocycles

# A design space for RFBs



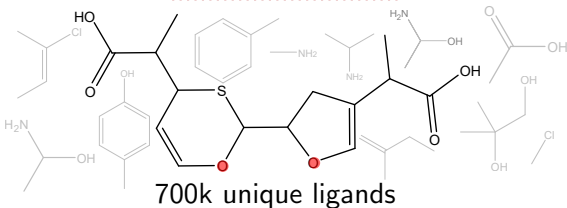
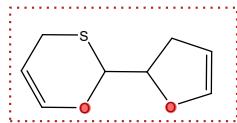
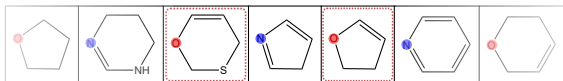
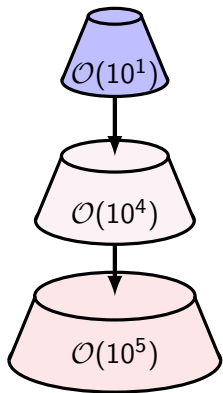
40 heterocycles

# A design space for RFBs

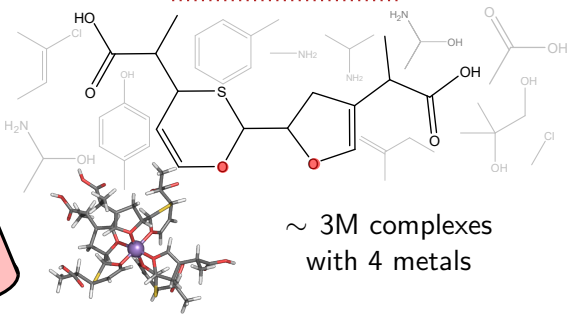
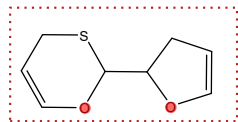
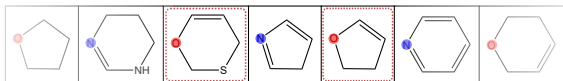
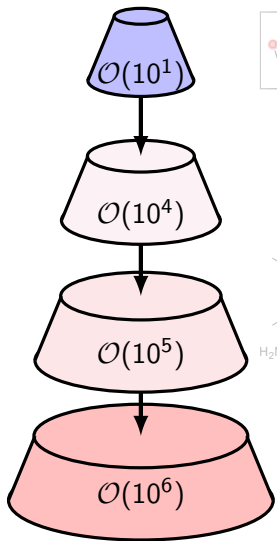


800 base ligands

# A design space for RFBs



# A design space for RFBs



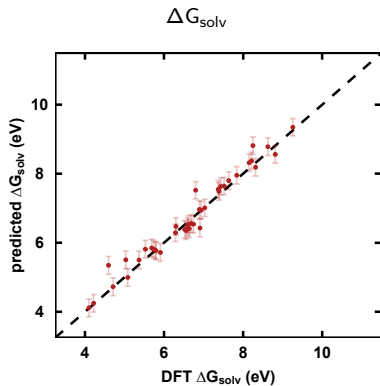
# Multiobjective optimization

We can predict quantities of interest for our RFBs:



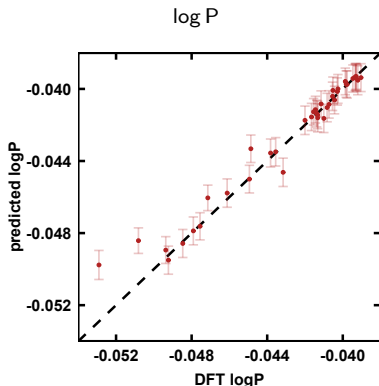
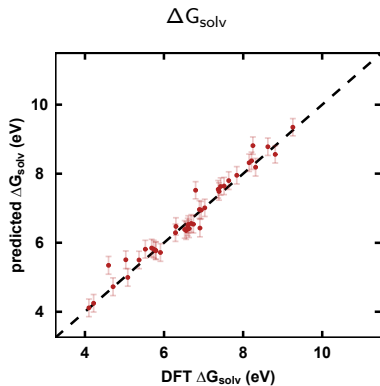
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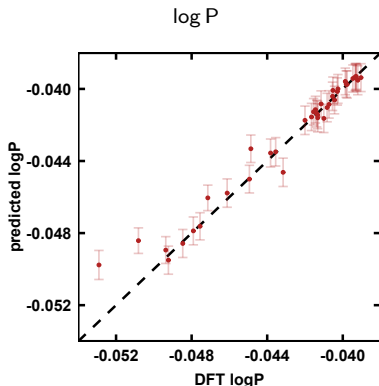
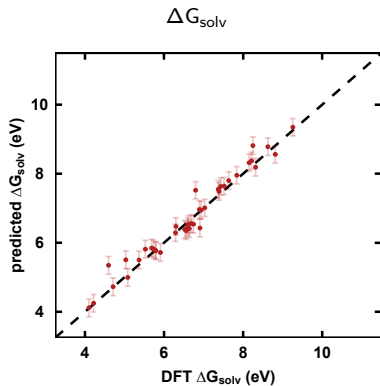
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# Multiobjective optimization

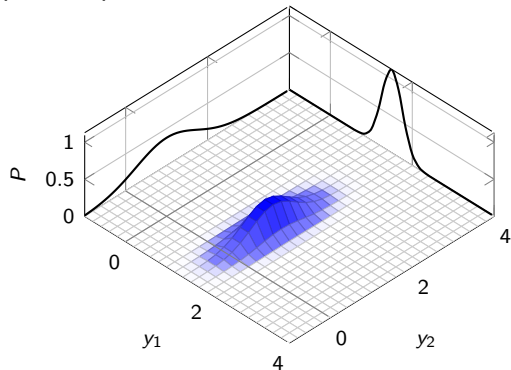
We can predict quantities of interest for our RFBs:



$$\begin{bmatrix} \Delta G_{\text{solv}} \\ \log P \end{bmatrix} = \begin{bmatrix} \hat{y}_1 \\ \hat{y}_2 \end{bmatrix} \sim \mathcal{N} \left( \begin{bmatrix} \hat{\mu}_1 \\ \hat{\mu}_2 \end{bmatrix}, \begin{bmatrix} \hat{\sigma}_1^2 & 0 \\ 0 & \hat{\sigma}_2^2 \end{bmatrix} \right)$$

# Multiobjective optimization

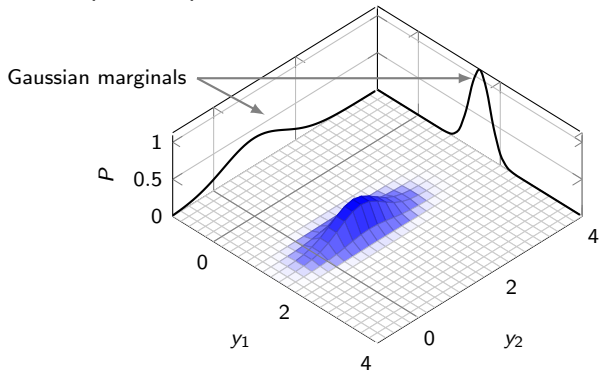
We can predict quantities of interest for our RFBs:



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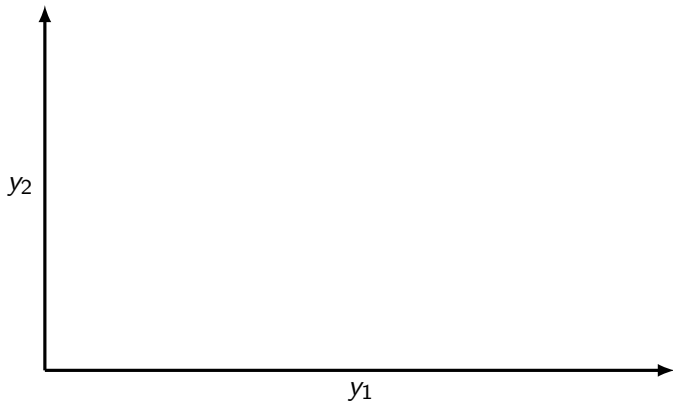
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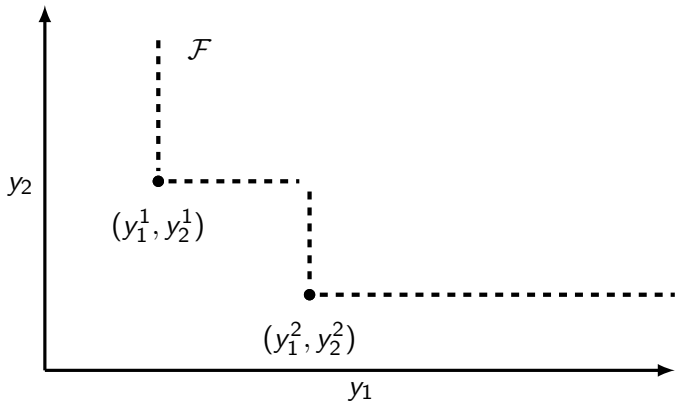
## 2D EGO Illustration

We will use a multiobjective expected improvement framework:



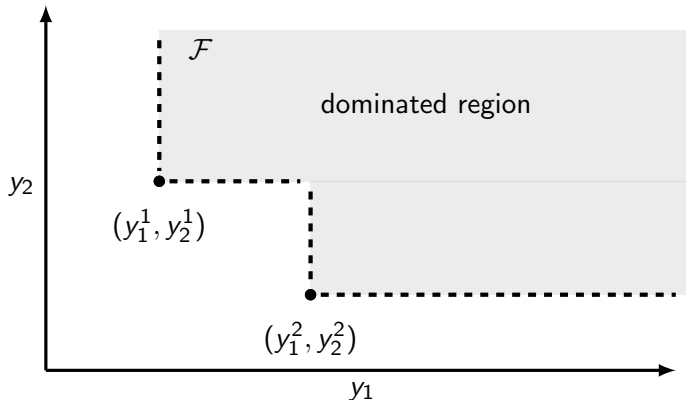
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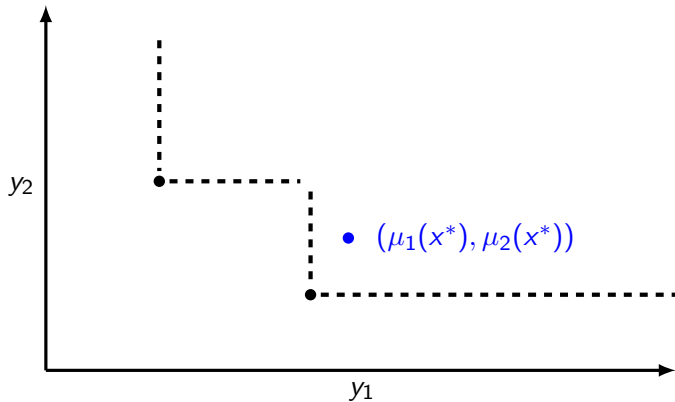
We will use a multiobjective expected improvement framework:





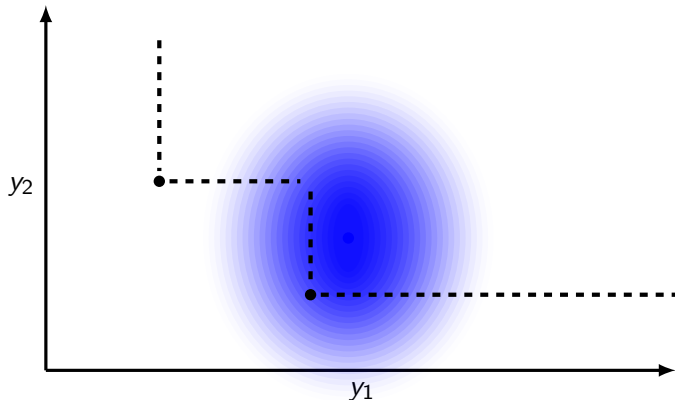
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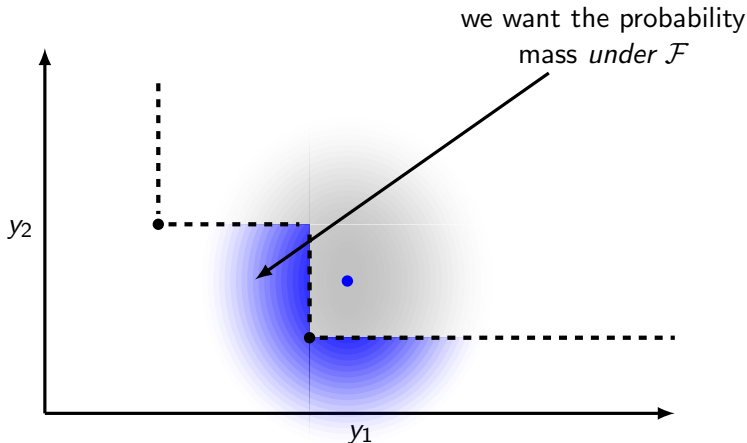
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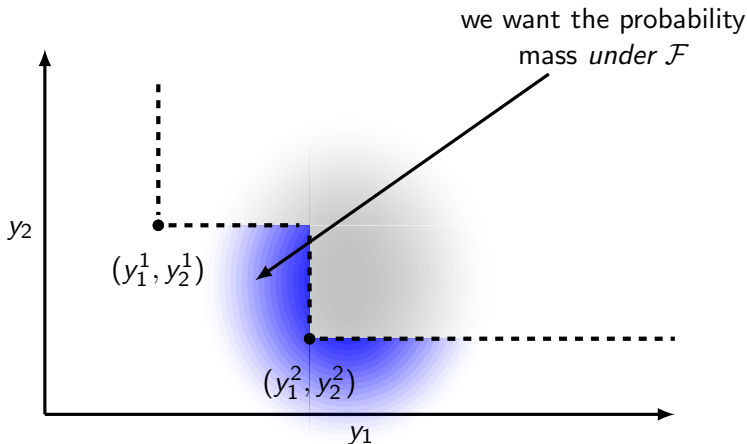
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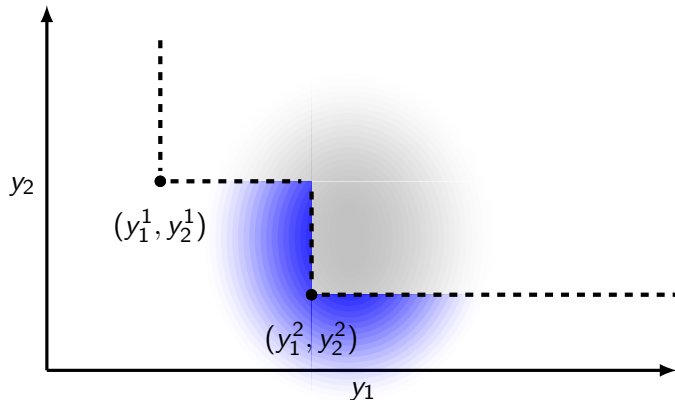
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We will use a multiobjective expected improvement framework:

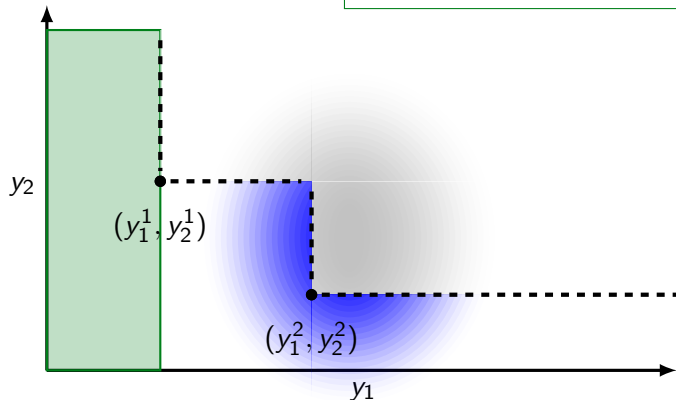
$$P(I) =$$



## 2D EGO Illustration

We will use a multiobjective expected improvement framework:

$$P(I) = \int_{-\infty}^{y_1^1} \int_{-\infty}^{\infty} p(\hat{y}_1(x^*), \hat{y}_2(x^*)) dy_1 dy_2$$

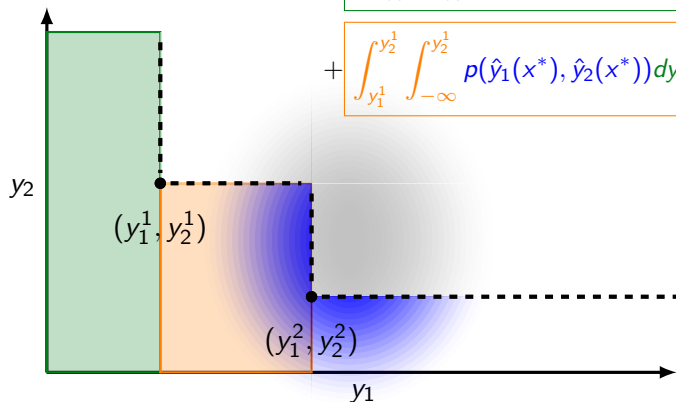


## 2D EGO Illustration

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$$P(I) = \int_{-\infty}^{y_1^1} \int_{-\infty}^{\infty} p(\hat{y}_1(x^*), \hat{y}_2(x^*)) dy_1 dy_2$$

$$+ \int_{y_1^1}^{y_2^1} \int_{-\infty}^{y_2^1} p(\hat{y}_1(x^*), \hat{y}_2(x^*)) dy_1 dy_2$$



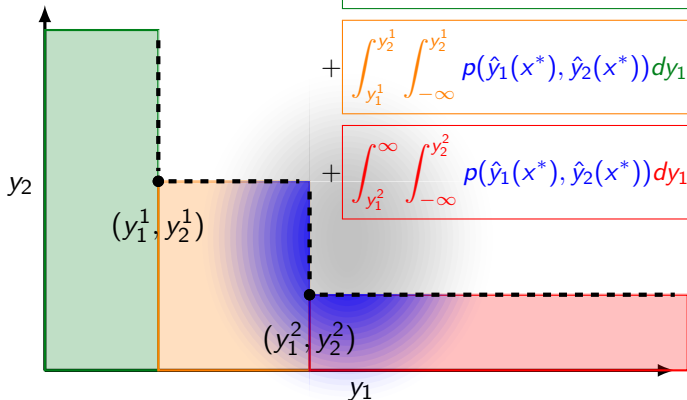
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$$+ \int_{y_1^2}^{\infty} \int_{-\infty}^{y_2^2} p(\hat{y}_1(x^*), \hat{y}_2(x^*)) dy_1 dy_2$$





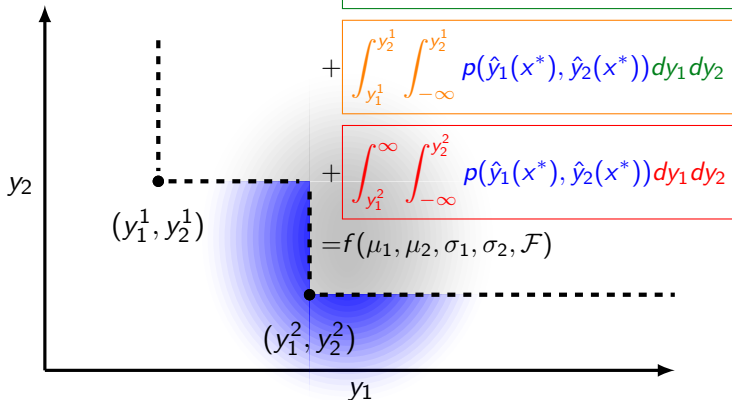
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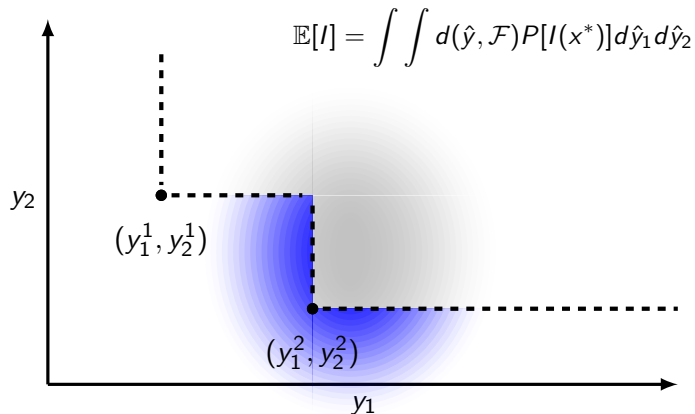
$$+ \int_{y_1^1}^{y_2^1} \int_{-\infty}^{y_2^1} p(\hat{y}_1(x^*), \hat{y}_2(x^*)) dy_1 dy_2$$

$$+ \int_{y_1^2}^{\infty} \int_{-\infty}^{y_2^2} p(\hat{y}_1(x^*), \hat{y}_2(x^*)) dy_1 dy_2$$



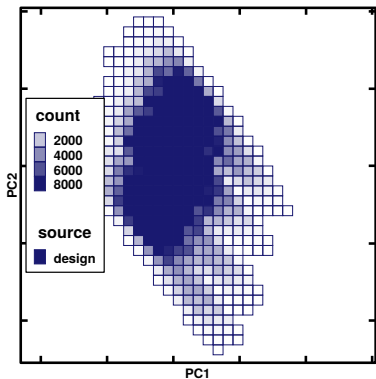
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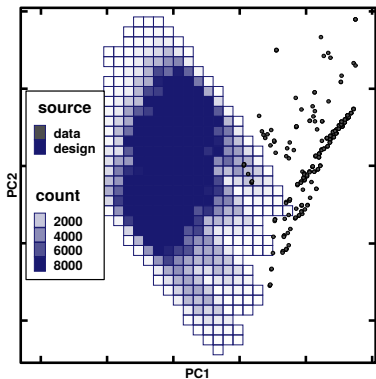
# Design space and clustering

We jump start with diversity-oriented cluster:



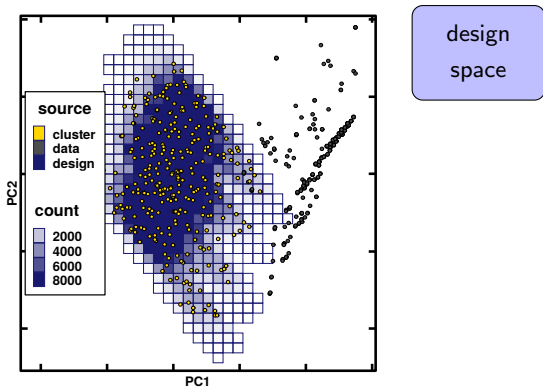
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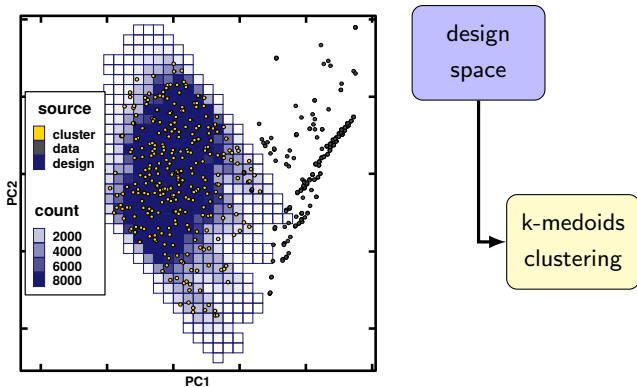
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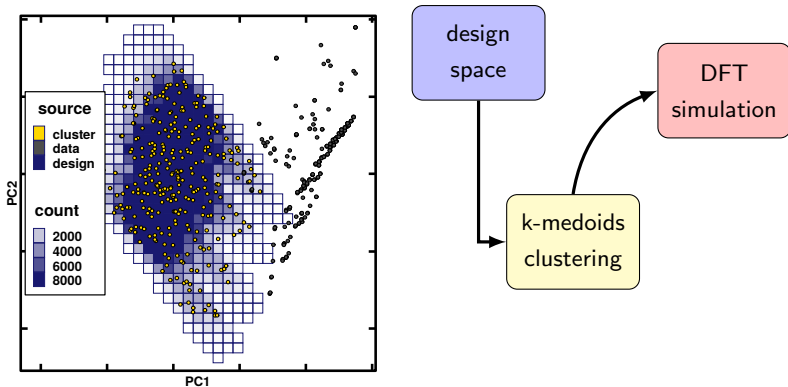
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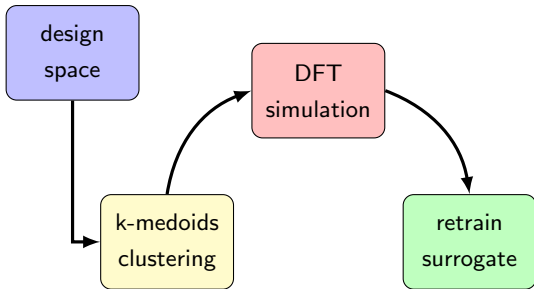
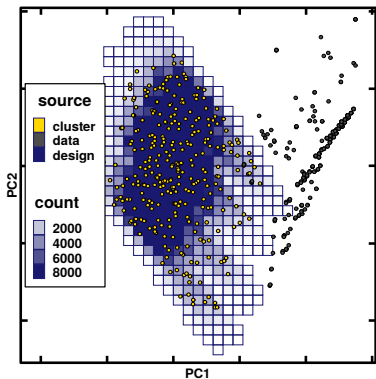
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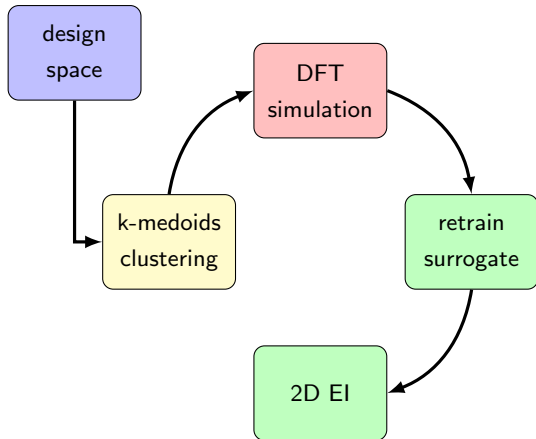
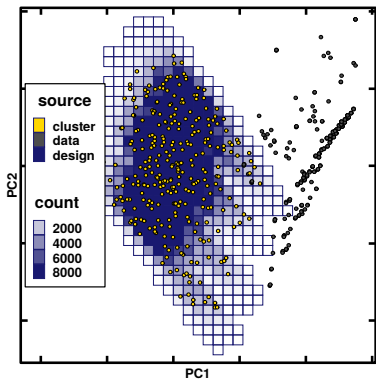
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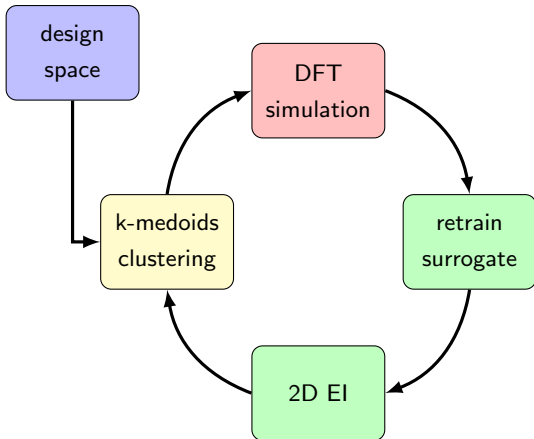
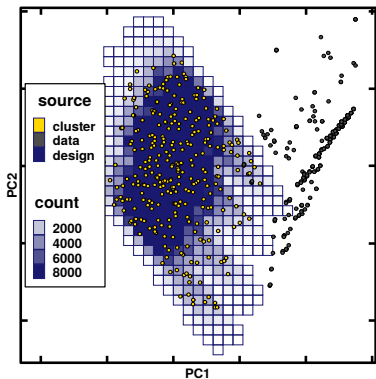
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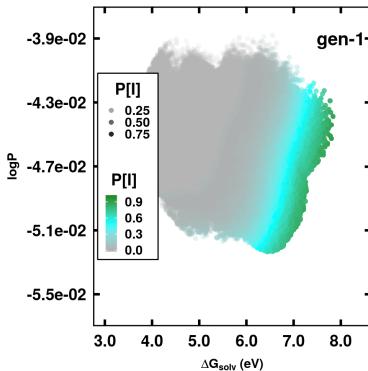
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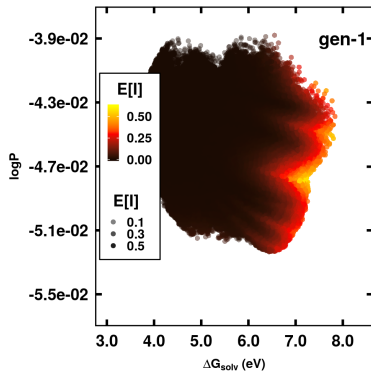


## EGO results

probability of improvement

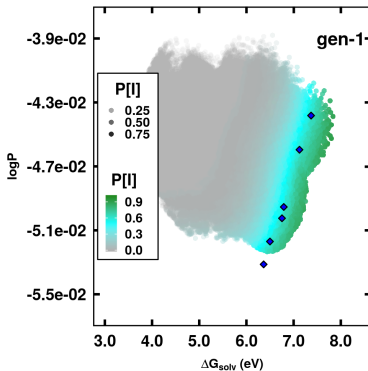


expected improvement

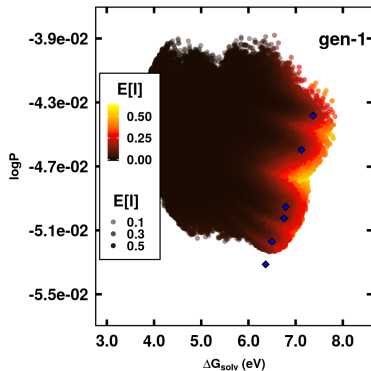


## EGO results

probability of improvement

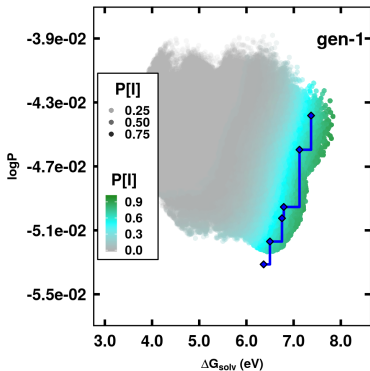


expected improvement

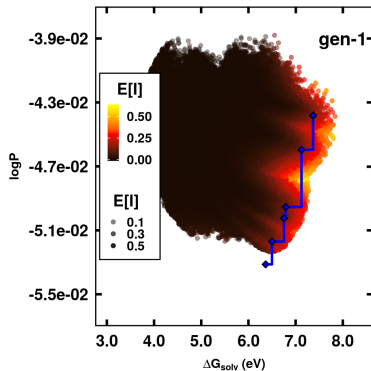


## EGO results

probability of improvement

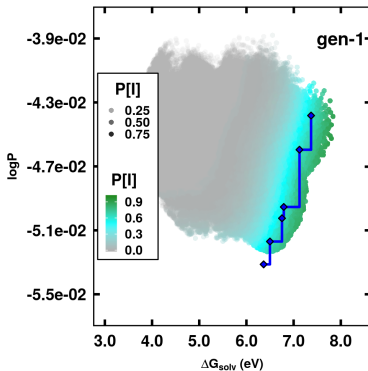


expected improvement

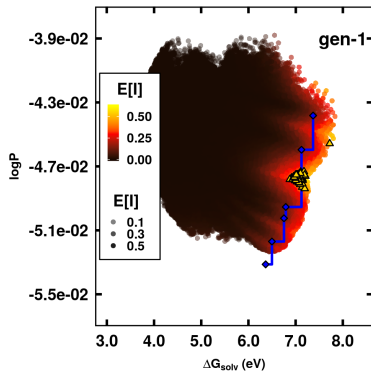


## EGO results

probability of improvement



expected improvement

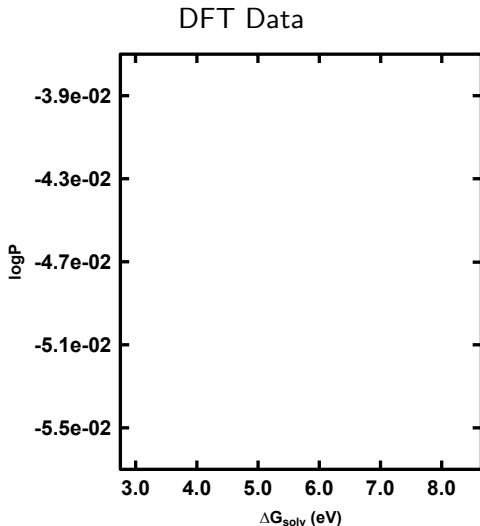


# EGO results

probability of improvement

expected improvement

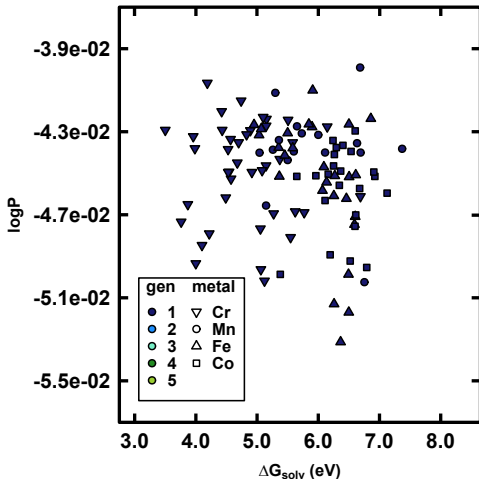
# DFT results





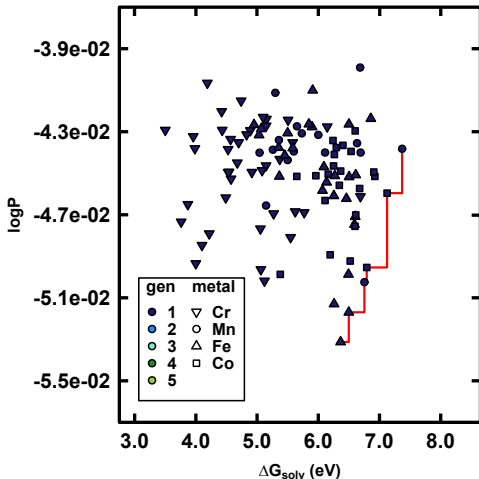
# DFT results

k-medoids points (generation 1)



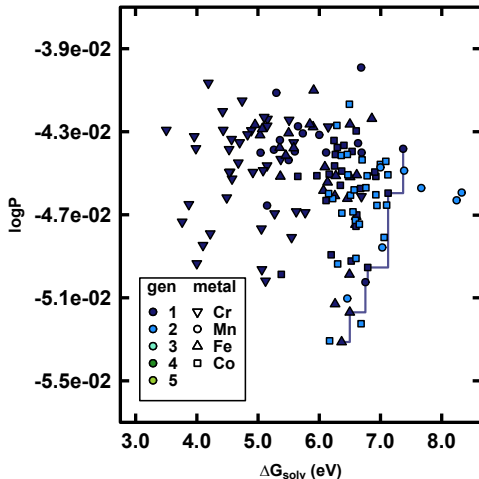
# DFT results

pareto front (generation 1)



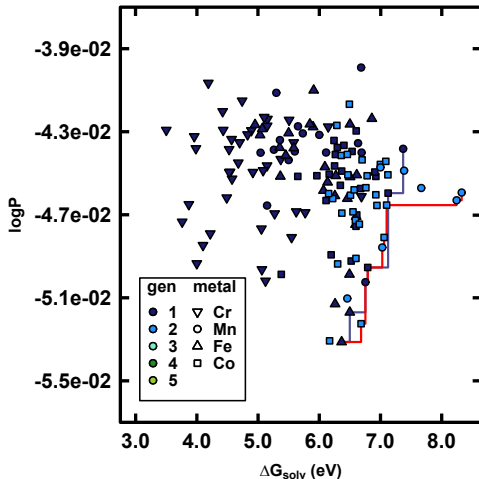
# DFT results

## El points (generation 2)



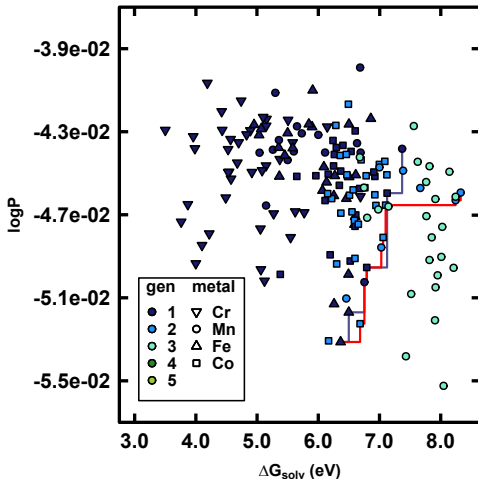
# DFT results

pareto front (generation 2)



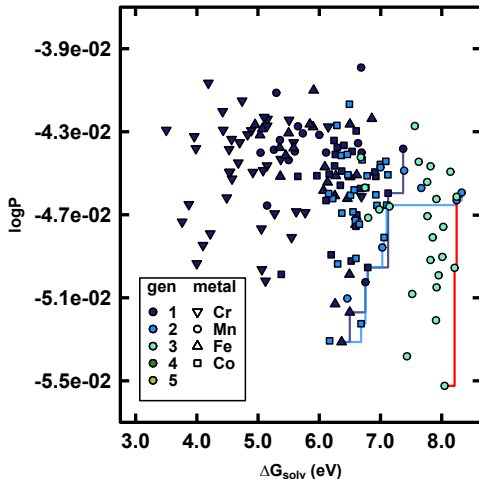
# DFT results

## El points (generation 3)



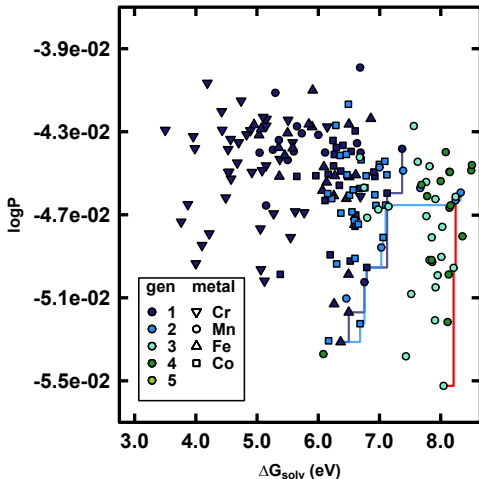
# DFT results

pareto front (generation 3)



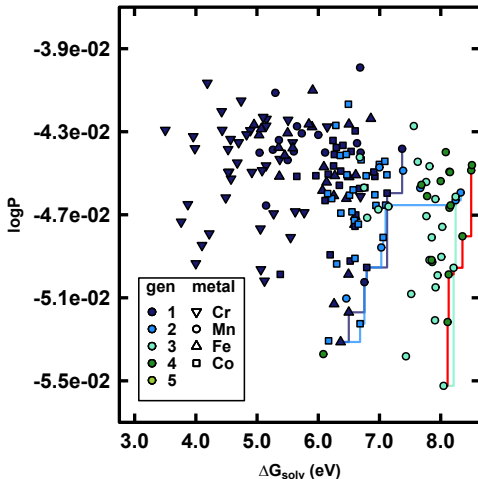
# DFT results

## El points (generation 4)



# DFT results

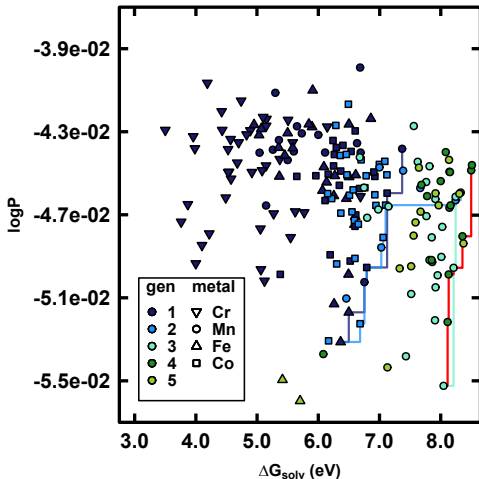
pareto front (generation 4)





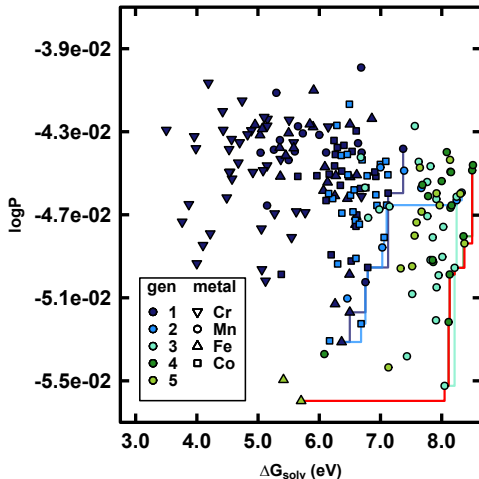
# DFT results

## El points (generation 5)

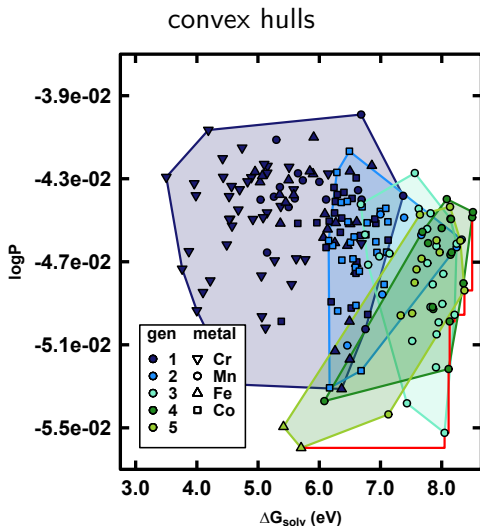


# DFT results

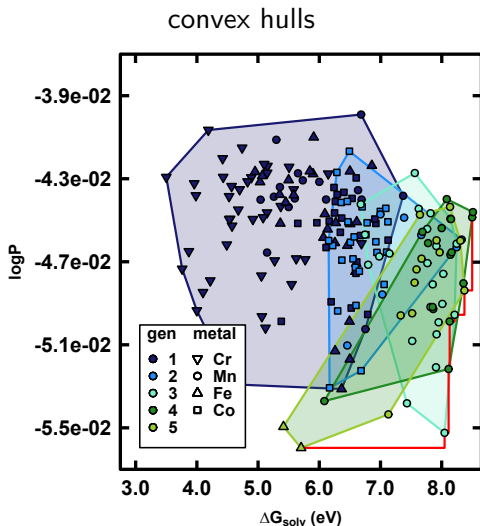
pareto front (generation 5)



## DFT results

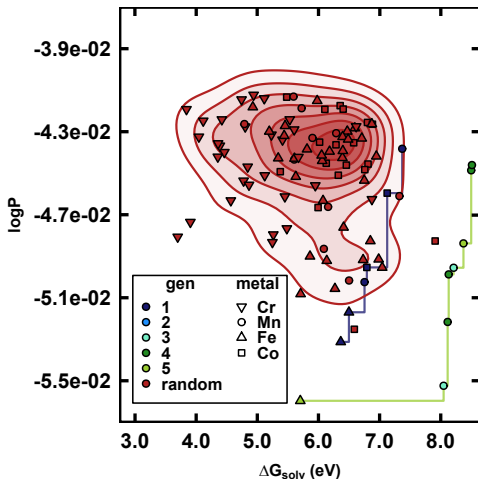


## DFT results



# DFT results

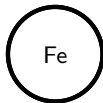
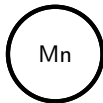
comparison to random sampling



# Final lead analysis

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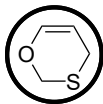
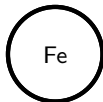
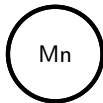
metal  
center



# Final lead analysis

metal  
center

6-member  
heterocycle



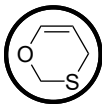
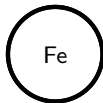
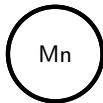


# Final lead analysis

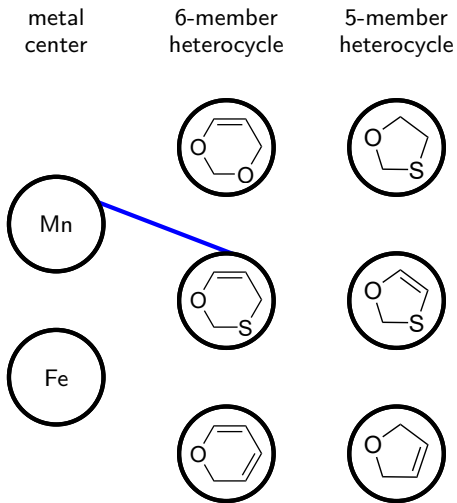
metal  
center

6-member  
heterocycle

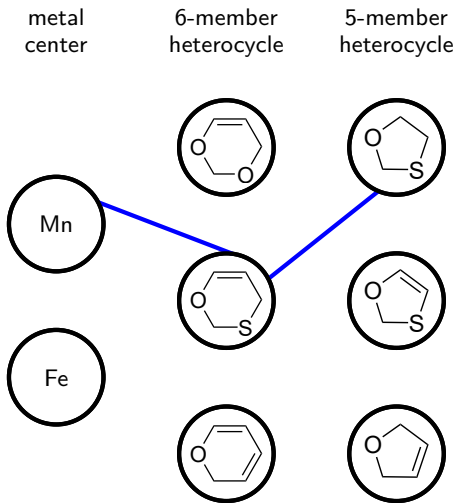
5-member  
heterocycle



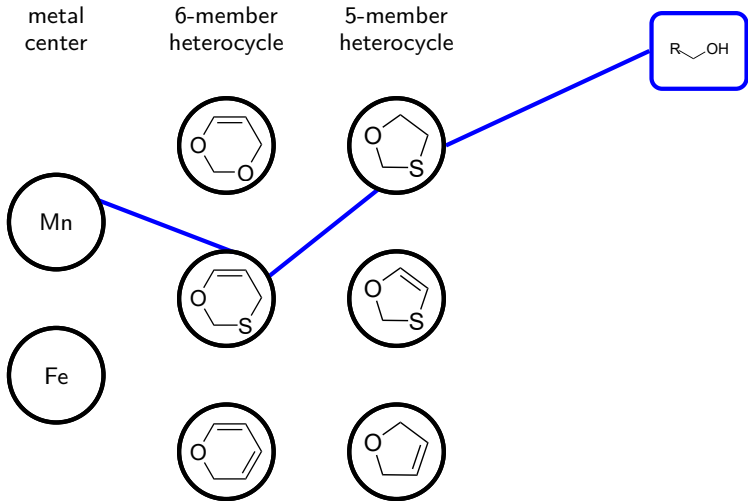
# Final lead analysis



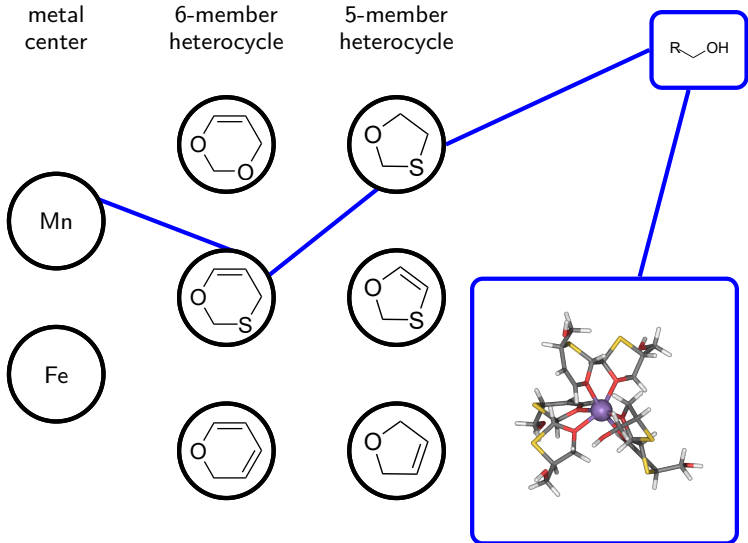
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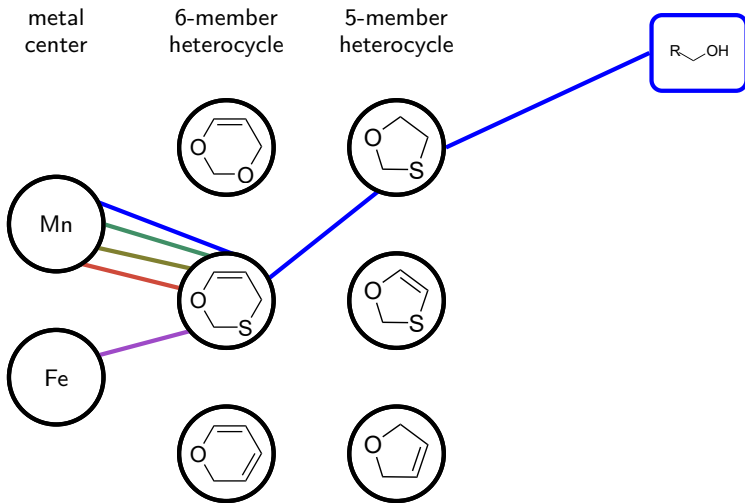
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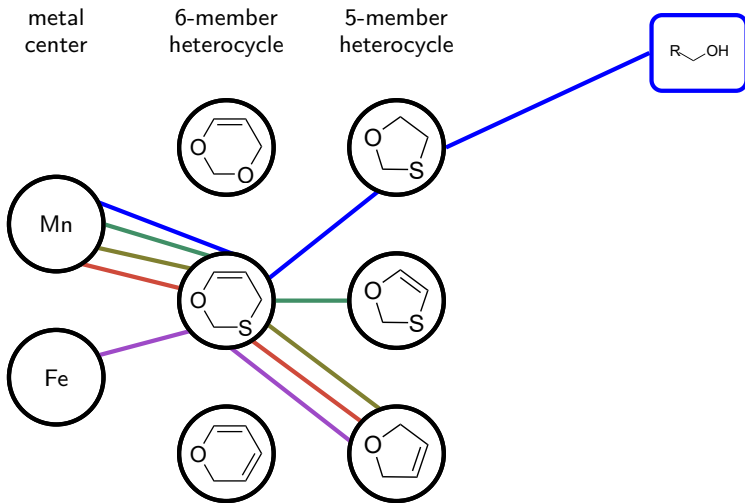
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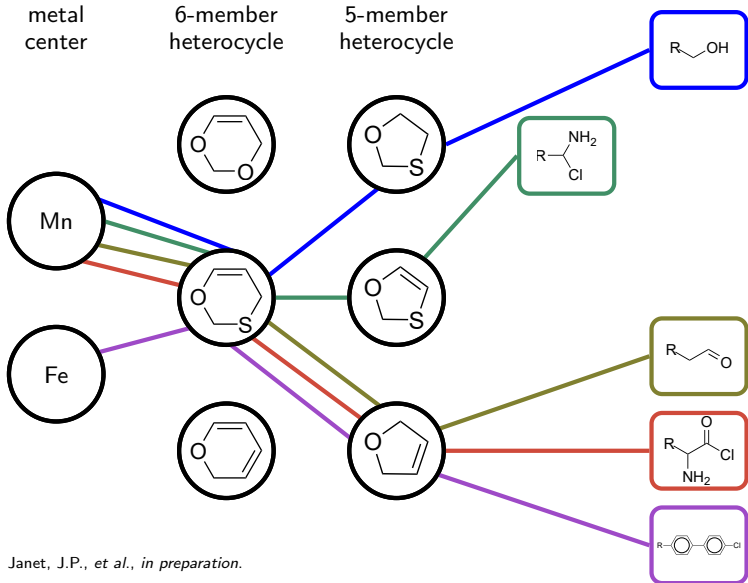
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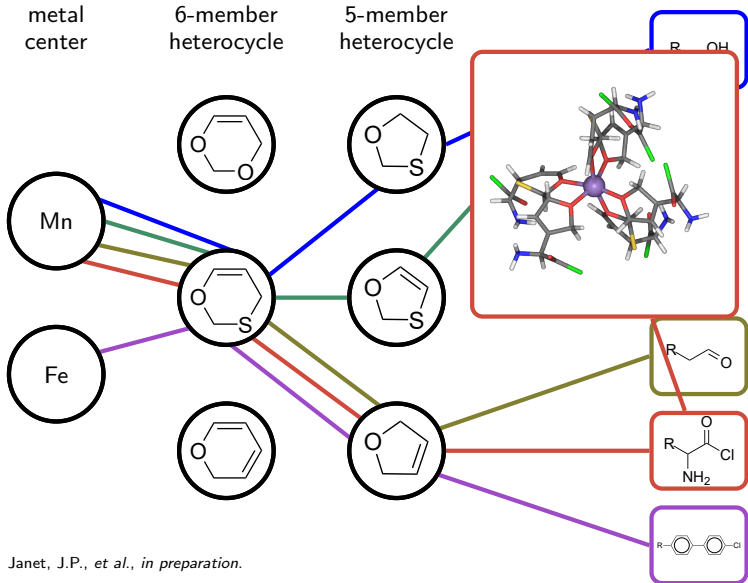
# Final lead analysis



Janet, J.P., et al., in preparation.

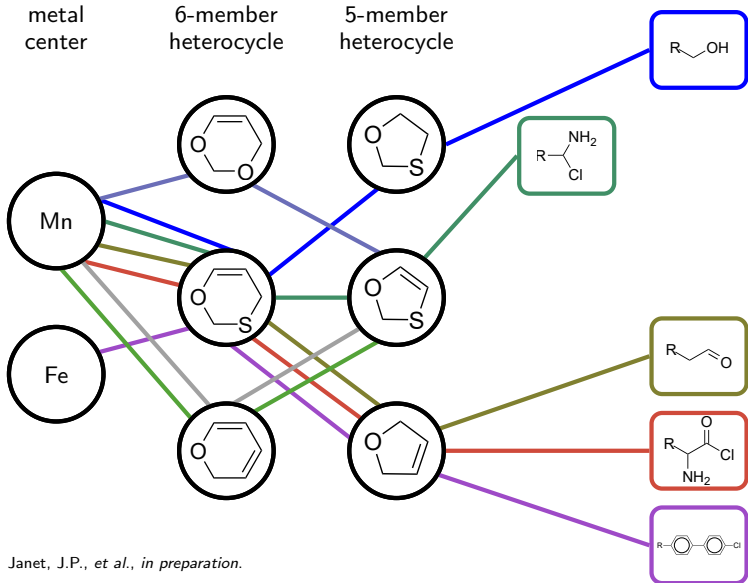


# Final lead analysis



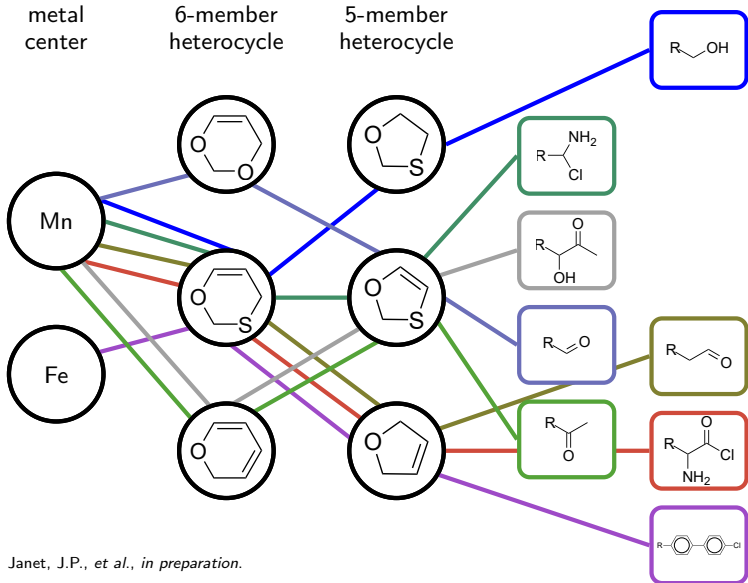
Janet, J.P., et al., in preparation.

# Final lead analysis



Janet, J.P., et al., in preparation.

# Final lead analysis

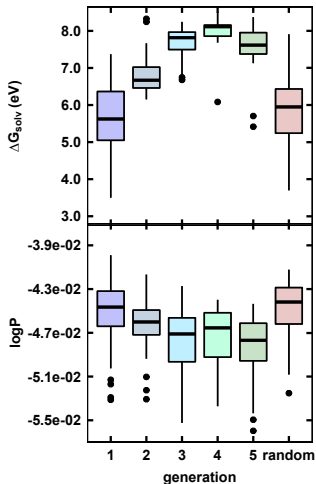


Janet, J.P., et al., in preparation.

# Case study conclusions

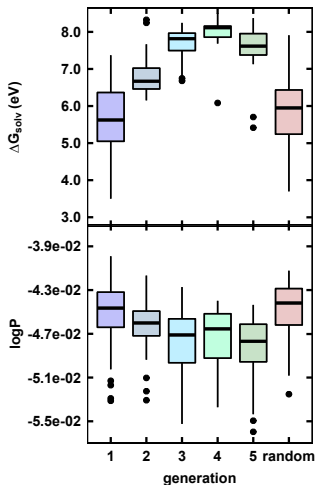
# Case study conclusions

- EI framework provides high resolution in the region of interest (c.f. maximum uncertainty), converges quickly



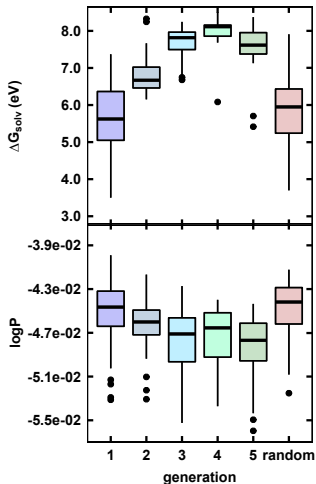
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## Case study conclusions

- EI framework provides high resolution in the region of interest (c.f. maximum uncertainty), converges quickly
- We are able to identify fruitful regions from large chemical spaces based on few DFT evaluations
- Multiobjective DFT optimization guided by data-driven method efficiency generates lead complexes



# Acknowledgments

Thanks to the Kulik group and funding partners:

